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Transient flow boiling in a semi-annular duct: From the Onset of Nucleate Boiling to the Fully Developed Nucleate Boiling

V. Scheiff, N. Baudin, P. Ruyer, J. Sebilleau, C. Colin

Abstract

This paper presents an investigation of the transient Onset of Nucleate Boiling (ONB) on a vertical heated surface cooled by an upward flow. The duct geometry used (semi-annulus with a heated inner wall) make this study very similar to a fuel rod in a Pressurised Water Reactor (PWR). This test section is then heated with different power steps to show the ONB and observe its propagation along the wall.

The fluid used is the refrigerant HFE7000 flowing with flow rates corresponding to Reynolds numbers from 0 to 60,000 and subcoolings Jakob numbers from 8 to 33. Synchronised infra-red (IR) thermal measurements and high-speed camera visualizations provided new data which helped to develop models to characterise the Onset of Nucleate Boiling and the transition to the Fully Developed Nucleate Boiling regime (FDNB).

This very finely characterized local behaviour provides an original insight for the onset of nucleate boiling in such sub-cooled convective configuration. It is shown that boiling is initiated by nucleation at a few specific sites and then propagates in the wake of a large vapor pocket flowing along the wall. Analysis of wall to fluid heat transfer evidences a short heat transfer degradation phase below the first vapor pocket, followed by a very effective cooling in its wake. The wall to fluid heat transfer during this transition toward fully developed nucleate boiling appears uncorrelated to the power dissipated within the heating element or to flow conditions.

1. Introduction

The core of a Pressurised Water Reactor (PWR) contains thousands of cylindrical fuel rods immersed in high pressure water that acts as coolant and moderator fluid. Through the net of fuel rods some control rods regulate the nuclear reaction but an accidental ejection of one of these control rods could lead to a local and sudden reactivity increase, namely a reactivity initiated accident (RIA), resulting in a large increase of the fuel rod temperature. While the rod temperature increases at a rather large heating rate (hundred of K/s), the heat transfer from its clad to the surrounding fluid is first characterized by convective heat transfer, and then boiling heat transfer. There is still a lack of knowledge for the rod’s clad to coolant heat transfer in those transient conditions. The present study takes part of the research program defined by IRSN (Institut de Radioprotection et de Sûreté Nucléaire) on this topic.

Transient boiling has been studied since the 1950s and most of these investigations were performed in pool boiling condition using ribbon [1], wire [2–4] or plate [5–7] heaters. Visentini [8] studied transient pool boiling in semi-annular geometry that is closer to the typical geometry encountered in a PWR. These studies point out that the boiling incipience, corresponding to the apparition of the first vapor bubble and generally denoted as onset of nucleate boiling (ONB), occurs with a wall superheat \((T_w - T_{sat})\) that increases with the heating rate and the subcooling. Sakurai et al. [2], Jonhson [9], Su et al. [7] used a modified Hsu’s criterion to predict the superheat at ONB with a good agreement with their experiments. These studies also report different boiling regimes during the transition from the ONB to the fully developed nucleate boiling regime (FDNB) or to the film boiling regime. In particular, and depending on the experimental condition, a temperature overshoot (OV), i.e. a temperature larger than the FDNB temperature, can be observed during this transition. The case of transient boiling with forced convection has also been studied on ribbon [9], wire [10] and plate [11] heaters. Johnson [9] pointed out an increase of the ONB superheat with the heating rate as observed for pool boiling. Su et al. [7] did not report measurement of the ONB...
The objective of this work is to understand and to model the incipience of the nucleate boiling in an upward semi-annular flow with an inner wall heated at different heating rates. In order to study the ONB in our experiment, the wall is heated by Joule effect. This was done for different Reynolds numbers and sub-cooling in the continuity of the studies initiated by Visentini et al. [12].

Although there were several studies about the transient boiling, especially in pool boiling, not all the physical mechanisms are understood. Moreover, except for Visentini et al. [12] study in pool boiling, none of the previous studies were made in a geometry similar to the one found in a nuclear core. The latter is idealized as a flow in an annular cross section with equivalent hydraulic diameter of the typical sub-channel defined between neighboring rods (in yellow in Fig. 1). To conduct experiments in a simple geometry but similar to this sub-channel, an experimental set-up was designed by Visentini et al. [12]. To measure the wall temperature with a high temporal and spatial resolution, the infra-red thermography was used and so an optical access to the wall was needed. Therefore a half-annular cross section with the heated inner half cylinder has been preferred to the annular one.

The objective of this work is to understand and to model the incipience of the nucleate boiling in an upward semi-annular flow with an inner wall heated at different heating rates. In order to study the ONB in our experiment, the wall is heated by Joule effect. This was done for different Reynolds numbers and sub-cooling in the continuity of the studies initiated by Visentini et al. [12].

1 For interpretation of color in Figs. 1 and 7, the reader is referred to the web version of this article.

2 Experimental set-up and measurements techniques

In this section, we introduce the main features of the facility. More details can be found in [12]. The test section has a semi-annular shape. The inner half cylinder consists of a 50 μm thick stainless steel foil heated by Joule effect. Its diameter is 8.4 mm and its length 200 mm. The outer part consists of a 34 mm internal diameter glass half cylinder (Fig. 2). The semi-annular section is filled with a coolant 1-methoxyheptafluoropropane (C₇F₇OCH₃), which will be referred as HFE7000 (3 M). This fluid has been chosen because of its low saturation temperature (35°C at atmospheric pressure), its low latent heat of vaporisation (ten times smaller than the water one), and the smaller critical heat flux value compared to water. These characteristics have been chosen to

<table>
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<th>Nomenclature</th>
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<td>Greek symbols</td>
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<td>( \alpha )</td>
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<tr>
<td>( \lambda )</td>
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<td>( \delta_c )</td>
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Subscripts |
exp | experimental |
FDNB | fully developed nucleate boiling |
ODB | Onset of Driven Boiling |
ONB | Onset of Nucleate Boiling |
| p | paint |
sat | saturation |
simul | simulated |
stat | stationary |
th | theoretical |
| w | wall |

For interpretation of color in Figs. 1 and 7, the reader is referred to the web version of this article.
perform highly transient boiling experiments with a lower power than required for water. The main physical properties of HFE7000 at saturation temperature and atmospheric pressure are given in the Table 1, where \( \rho \), \( C_p \), \( \lambda \) and \( v \) are the density, heat capacity, thermal conductivity and kinematic viscosity, respectively. \( h_v \) is the latent heat of vaporisation and \( \sigma \) the surface tension of the fluid. Physical properties of water at 155 bar are given in the Table 1 for comparison.

The metal half-cylinder is glued to two lateral quartz glass plates (thickness: 3 mm, width: 42 mm, length: 200 mm). The plates, together with the foil, are placed in an aluminium cell. In this cell, a visualization box filled with HFE7000 is used to reduce optical distortions.

![Fig. 2. Schema of the test section.](image)

**Table 1**

<table>
<thead>
<tr>
<th>Solid</th>
<th>Foil properties at 20 °C (stainless steel AISI 304)</th>
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<tbody>
<tr>
<td></td>
<td>( \rho_f ) (kg m(^{-3}))</td>
<td>( C_p ) (J kg(^{-1}) K(^{-1}))</td>
<td>( \lambda ) (W m(^{-1}) K(^{-1}))</td>
<td>( \sigma ) (N m(^{-1}))</td>
<td>( E_p ) (J K(^{-1}) m(^{-1}) s(^{-1/2}))</td>
<td>( E_v ) (J K(^{-1}) m(^{-1}) s(^{-1/2}))</td>
<td>( E_w ) (J kg(^{-1}) m(^{-1}) s(^{-1/2}))</td>
<td>( q_w ) (W m(^{-1}))</td>
<td>( q_v ) (W m(^{-1}))</td>
<td>( q_l ) (W m(^{-1}))</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Solid</td>
<td>( 7930 )</td>
<td>( 500 )</td>
<td>( 16.18 )</td>
<td>( 7.3 \times 10^{-8} )</td>
<td>( 480 )</td>
<td>( 25 )</td>
<td>( 30 )</td>
<td>( 30 )</td>
<td>( 30 )</td>
<td>( 30 )</td>
<td></td>
<td></td>
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</tr>
<tr>
<td>Fluid</td>
<td>( 1200 )</td>
<td>( 1480 )</td>
<td>( 0.13 )</td>
<td>( 8 \times 10^{-10} )</td>
<td>( 4.2 \times 10^{-7} )</td>
<td>( 4.8 \times 10^{-7} )</td>
<td>( 4.8 \times 10^{-7} )</td>
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The experiments are carried out in flow boiling conditions by inserting the test cell in a two-phase flow loop consisting of a gear pump, a Coriolis flow meter, a pre-heater, a 1 m long channel upstream the test section to establish the flow and a condenser. The inlet temperature and pressure of the test section are measured by a thermocouple and an absolute pressure transducer. The flow-rates investigated vary from 0.1 to 0.3 l s\(^{-1}\) corresponding to mass fluxes from 323 to 969 kg m\(^{-1}\) s\(^{-1}\) and corresponding to Reynolds numbers from 14,000 to 60,000. The velocity profiles in the test section in single-phase flow have been measured by PIV in the mid-plane and characterized in the whole test section by numerical simulations by Baudin et al. [13]. The inlet fluid temperature is controlled by a chiller THERMOTEK P805, and the subcooling investigated vary from 5 to 20 K. So the sub-cooling dimensionless Jakob number, defined as \( \text{Ja}_{\text{sub}} = \frac{\rho C_p h_v}{\rho \sigma} \), represents the amount of energy required to heat up a mass of liquid from \( T_s \) to \( T_{sat} \) normalized by the energy required to vaporize the same mass of liquid. In our context, the larger the Jakob number, the higher the condensation rate in the bulk or the larger the delay for wall nucleation favourable conditions. The electrical power is provided by a power supply SORENSEN SGA. It covers the 0–40 V voltage range and the 0–250 A current range. The power supply is driven by an arbitrary generator to impose power steps of different powers and durations. The power supply can provide a current increase up to 45 A s\(^{-1}\). A voltmeter and an ammeter measure the voltage \( U \) and current \( I \) to calculate the generated power in the metal foil \( P = UI \).

Finally in a PWR, the refrigerant used is water. The thermodynamic conditions are \( P = 155 \) bars and \( T \in [300–1500] °C \) with a cylinder fuel rod with an internal radius \( r_i = 4.8 \) mm and external radius \( r_e = 7 \) mm. The Reynolds number is equal to 400,000. In our model set-up, the fluid used is the HFE7000. The thermodynamic conditions are \( P = 1 \) bar and \( T \in [20–300] °C \) with a semi-annulus section with an internal radius \( r_i = 4.2 \) mm and external radius \( r_e = 17 \) mm. The Reynolds number is between 0 and 60,000. There are differences between normalized numbers (Nusselt or Reynolds number …) but the goal of our experiment was to be able to study the transient boiling with simplified conditions.
and reach every boiling regimes with a limited required electrical power.

2.1. Wall temperature measurements

Measurements are performed with an infra-red camera looking at the foil from backward (see Fig. 2). A CEDIP JADE III camera with a sensitivity range between 3.5 and 5.1 μm is used. It has a focal plane array detector cooled by a Stirling MCT. For this study, the acquisition frequency is 500 fps and the height of the metal foil investigated is about 7 cm in the z direction (Fig. 2). The integration time is between 20 and 500 μs for a spatial resolution of 240 × 320 px². The infra-red camera is calibrated thanks to a DCN 1000 N4 black body. The uncertainties on the measurement temperature of the black surface depend on the temperature range of calibration. For a low temperature range calibration (20–100 °C), the uncertainty is about ±0.6 °C at 20 °C and ±0.1 °C at 100 °C. For a high temperature range calibration (20–250 °C), the uncertainty is about ±3 °C at 20 °C but only ±0.3 °C at 250 °C. These uncertainties take into account the non uniformity of the black body temperature surface and the noise on the camera sensor. The temperature and the heat flux measurements are made on the area between 5 and 15 cm from the bottom of the heated foil (≈ 3 – 8D0), each temperature measurement is averaged on 2 × 2 mm².

The thermal gradient across the foil thickness is expected to be negligible, since the Biot number Bi characterizing the thermal resistance of the foil by comparison to the thermal resistance of the environment.

Due to the small value of Bi, the foil temperature will be considered constant in the thickness. Moreover, the diffusion time across the foil thickness τ_diff = e_p / x_w = 0.6 ms, is actually small enough to assume that there is no time lag between the thermal evolution of both sides of the metal foil. The thermal effusivity E_w characterizes the ability of a material to exchange thermal energy with its environment.

To obtain sufficiently precise temperature measurements, the backside of the metal foil is covered with a layer (≈30 μm thickness) of black paint with large emissivity (0.94). The black paint used is a Belton Spectral RAL 9005 MAT BLACK paint, which thermal properties were measured by the company NeoTIM (Albi, France), and are given in Table 1. For a heat transfer coefficient of h = 6000 W m⁻² K⁻¹, the Biot number of the paint layer is Bi_p ≈ 1.2 (for a paint thickness of 30 μm), which means that a small temperature gradient can exist between the surface of the paint (IR camera side) and the metal foil. The diffusion time across the paint thickness is about τ_{diff} ≈ 0.01 s so some time lag can be expected.

We do not notice a significant change in the measurement of the resistance of heated foil without and with paint, so we made the assumption that the paint is not electrically conductive. In a previous study [8], 2D transient heat conduction in the metal foil (without the black paint layer) performed with COMSOL Multiphysics have shown that the conduction in the lateral direction remains very small. Thus a 1D transient conduction model inside the metal foil and the paint is used to characterize the effect of the paint on the thermal measurement (temperature gradient and time delay). Fig. 3 shows the result of this model for a paint thickness of 25 μm and a steady heat transfer coefficient of 1000 W m⁻² K⁻¹. As one can see the temperature gradient in the paint is small and becomes quickly negligible: except for strong temperature variations ((dT/dt)/(dT/dx) ≪ τ_{lag}), the temperature evolution on the paint side corresponds to the evolution on the liquid side with a lag time of about 0.05 s.

This model also shows that the heat flux from the wall to the fluid φ_w can be calculated using the simple thermal balance:

\[
\phi_w = \phi_{gen} - \left( \rho_w \ C_p \ e_w + \rho_p \ C_p \ e_p \right) \frac{dT_w}{dt}
\]

where \( \phi_{gen} \) is the wall temperature variation. The natural convection and radiation heat transfers between the air and the paint are neglected since the corresponding heat fluxes (< 400 W m⁻² for both) are small in comparison to the generated power (> 10 kW m⁻²).

A National Instruments box CompactRIO9035 is used to acquire the thermocouples (flow temperature control), pressure, flow and power measurements. The uncertainties of the electronic devices (ammeter, National Instrument box) are very low and of the order of magnitude of 0.1% (Visentini [8]). The power generated by Joule effect per surface unit \( \phi_{gen} \) is equal to \( U^2 L / l \) where L the length of the foil and l its width. The main uncertainty comes from the length of the part where the voltage is measured (about ±0.2 cm on 8.5 cm i.e. about 2%). Thus the total uncertainty on \( \phi_{gen} \) is 2.5%, which is also the uncertainty on the heat flux in steady state. The heat transfer from the wall to the fluid is calculated with
Eq. [1]. Assuming that $\rho_w C_{p,w} e_w + \rho_p C_{p,p} e_p = 242 \text{ J m}^{-2}$ has a low uncertainty (the thermal properties of the stainless steel and paint are known and in our range of temperature, the thermal inertia variation is 10% maximum). The absolute uncertainty on the heat flux is:

$$\langle \Delta q_w \rangle^2 = \left( \frac{\partial q_w}{\partial \phi_{gen}} \right)^2 \Delta \phi_{gen}^2 + \left( \frac{\partial q_w}{\partial T_w} \right)^2 \Delta T_w^2.$$  

The generated heat flux varies from 40 to 400 kW m$^{-2}$, and the temperature time derivative at the onset of nucleate boiling varies from 10 to 500 K s$^{-1}$. So the wall heat flux uncertainty can reach 6.5% of its value.

2.2. Transient convection

Baudin et al. [13] studied the turbulent flow and convection heat transfer in a semi-annulus through experiments and numerical simulations. The numerical simulations were made with the software StarCCM+ including the resolution of RANS equations using a k-ε model and resolution of the equation of the energy in the fluid and in the solid composed of the foil only. They observed that the wall temperature evolution is self-similar when scaled by the steady wall temperature and that transient regime is characterized by a time scale $t_c$ which depends only on the Reynolds number (through the Nusselt number).

These simulations were performed without a paint layer, and only the metal foil thermal mass characterizes the time scale evolution while, in their experiments, the metal foil was painted with a layer of thickness around 100 μm. Thus, experimentally, the wall thermal mass was high ($\approx 178$ J m$^{-2}$ K$^{-1}$) and induced uncertainties on the heat transfer coefficient at the beginning of the heating. In the present study the paint thickness is about 30 μm, the wall thermal mass is thus low ($\approx 44$ J m$^{-2}$ K$^{-1}$) and the uncertainty on the heat transfer coefficient during the first times is low.

The experimental wall temperature and the dimensionless heat transfer coefficient evolutions during a power step are plotted respectively on the left hand side and right hand side in Fig. 4. This measurement is an average temperature at the top of the foil (height = 0–3.5 cm) in the central part of the metal foil to avoid entrance phenomenon.

At the beginning of the heating, the thermal boundary layer is not established yet, thus the heat transfer coefficient is higher than in steady state. For both the heat transfer coefficient evolution and the wall temperature evolution, the characteristic time to reach steady state decreases when the Reynolds number increases. However, while the wall temperature is steady after about 1–5 s, the heat transfer coefficient is steady after about 0.2–0.75 s.

The advection time defined with the length of the heating surface and the average velocity is:

$$\tau_{adv} = \frac{L}{\bar{U}} = 0.15–0.5 \text{ s}$$  

with the average velocity $\bar{U} = 0.1–0.7 \text{ m s}^{-1}$ for $Q = 0.05–0.41 \text{ s}^{-1}$. The turbulent mixing time can be estimated from an estimate of the typical eddies length $L_{eddies}$ by:

$$\tau_{mix} = \frac{L_{eddies}}{\bar{U}} = \frac{k \Delta dh}{U} = \frac{8.2 \Delta dh}{0.05 \bar{U}} = 0.11 – 1.3 \text{ s}$$  

with the constant of Von Karman $\kappa = 0.41$.

The advection characteristic time $\tau_{adv}$, taken at the center of the flow, is lower than the forced convection times measured. Due to inlet flow, the flowing liquid temperature is kept constant and equal to the sub-cooling temperature imposed in the hydraulic loop.

The characteristic times of mixture $\tau_{mix}$ are in good agreement with the times obtained experimentally. The vortices in the mixture contribute to the development of the thermal boundary layer and are therefore characteristic of the forced convection regime establishment. In this case, the heating rates imposed during this regime are low and the heat transfer is not due to unsteady conduction but rather to the forced convection since the eddies control this regime. The heat transfer coefficient characteristic time is thus directly related to a turbulent time scale.

Baudin et al. [13] pointed out a linear decrease of $dT_{wall}/dt$, thus, a quasi-steady evolution of the wall temperature can be assumed (i.e. assuming $h = h_{stat}$). This is indeed sufficient as long as we do not focus on the very first times of the transient. The heat transfer coefficient during a test achieved quickly its steady state since the paint thickness is low so:

$$\frac{T_w(t) - T_0}{T_{w,stat} - T_0} = 1 - e^{-t/\tau_h}$$  

$$\tau_h = \frac{M_h}{h_{stat}}$$

$h_{stat}$ is the steady convection heat transfer coefficient and $M_h = \rho_w C_{p,w} e_w$ is the thermal mass of the wall. Only the heated foil is considered in the simulations, the thermal mass is $M_{h,w} = \rho_w C_{p,w} e_w$. For the experiments, the paint layer is included: $M_{h,w,p} = \rho_w C_{p,w} e_w + \rho_p C_{p,p} e_p$. The good agreement between the

![Fig. 4. Evolution of the reduced wall temperature and the dimensionless heat transfer coefficient $h_{stat}/h_{stat}$.](image-url)
time scales calculated from the simulations/experiments with Eq. (6) is shown on Fig. 5. Although the steady state heat transfer coefficient in [13] was obtained for an area 13 cm away from the bottom of the foil, these values decrease or increase of maximum 2% on the studied area of this article. Therefore this value is kept to model the temperature evolution on this whole surface.

The thickness of the thermal boundary layer including the viscous and buffer layers has been obtained from the results of numerical simulations Baudin et al. [13] and is defined as $\tau_{\text{sim}}$. From the evolution of the wall temperature, $\tau_{\text{sim}}$ was deduced from Eq. (5).

3. Analysis of the onset of boiling

In all this section, we analyse in details the phenomena occurring during the transition from single-phase to nucleate boiling regime following a step in power starting from zero. The analysis focuses first on a single test condition, and all the time and/or space evolution refer to these test conditions:

Then the analysis is generalized to a set of test conditions that have been considered, varying the power level as well as the flow conditions. Flow rate corresponds to different colors: red: 0.1 s$^{-1}$, blue: 0.2 l s$^{-1}$, green: 0.3 l s$^{-1}$. Liquid bulk temperature correspond to different shapes. The sub-cooling of the inlet liquid flow $\Delta T = T_{\text{sat}} - T_i$ (that is also the initial wall temperature subcooling) is $\circ : \Delta T = 13 \, ^\circ C, \Box : \Delta T = 15 \, ^\circ C$ and $\Diamond : \Delta T = 17 \, ^\circ C$. Finally, the generated heat flux, $q_{\text{gen}}$ is between 40,000 and 80,000 W m$^{-2}$.

3.1. A generic time evolution for local wall temperature

All over the test section, and for any test condition that leads to the onset of boiling, the time evolution of wall temperature is rather similar. Such a typical process is illustrated on the graph of Fig. 6. As the power is set to its constant non-zero value (red symbol around $t = 1$ s on the graph), the wall temperature first increases from its initial value, that equals to the sub-cooled liquid temperature within the test section. It follows an exponential relaxation like for the purely single-phase tests described in Section 2.2: the blue part of the curve. It goes beyond the saturation temperature value (blue square) without any noticeable deviation until it reaches a maximum (the black dot, after the ONB) whose value corresponds to an overheat of approximately 40 $^\circ$C with respect to saturation temperature. Then a rather sharp decrease (the green dashed lines denoted overshoot on the graph) occurs over a fraction of a second. Temperature then reaches a quasi-constant level (the purple part of the curve around 50 $^\circ$C in this case) that is still over the saturation value and will be considered as the steady local temperature for such a test. Small perturbations of few degrees around a constant value can be seen on the curve. The rather low wall superheat corresponds to typical nucleate boiling regime.

From this analysis of the wall temperature, one clearly identifies two different stages in the transition from the initial to the final steady states: the increase, that is very similar to the transient convection, followed by a sharp decrease. The overshoot of temperature (i.e. the difference between the local transient maximal temperature and the final steady value) is relatively large, around 25 $^\circ$C, even larger than the wall superheat at the steady state (around 15 $^\circ$C).

3.2. Sketch of the two-phase flow pattern at the onset of boiling

On Fig. 7, several snapshots of the high speed camera are provided for a single test and at different times. The heated wall corresponds to the thick black area on the right hand side of each picture. The high-speed camera is placed perpendicularly to the infra red camera and takes pictures in the (x,z) as indicated in Fig. 2) and the high-speed camera visualizations are made by ombroscopy. The small hyphen indicates a 1 mm long scale. During the test, the metal foil is measured on a field of 20 $\times$ 120 pix$^2$ where 1 pixel is equal to 0.047 cm. So $10$ pixels for the diameter of a bubble during the nucleate boiling). It’s not the case for the high-speed Camera space resolution is sufficiently high with respect to the typical bubble size (~10 pixels for the diameter of a bubble during the nucleate boiling). It’s not the case for the infra-red camera where it’s not possible to see the bubble feet clearly. Finally, due to technical performance the High speed camera and infra-red camera sampling frequencies are 500 Hz which is not sufficient to see the first steps of the bubble nucleation (see Fig. 7).

The left hand side photo corresponds to the time, denoted $t_{\text{ONB}}$ at which the first deviation from the initial state has been catched by the ad hoc algorithm of image treatment. Only a zoom on the surrounded area could provide a clear evidence of an event for a direct visual observation. It is seen that 6 ms after (second picture), a vapor bubble of less than 1 mm thickness and a few mm long covers a part of the wall. It then grows or expands rapidly over

---

Fig. 5. Wall temperature characteristic time in forced convection, compared to theory, for experiments ($M_{h,w} = \rho \cdot C_p \cdot u \cdot w$) and simulations ($M_{h,w} = \rho \cdot C_p \cdot \alpha \cdot u$) versus the Reynolds number.

---

Fig. 6. Temporal evolution of wall temperature in the close vicinity of the first nucleation event.
the tens of ms after its apparition, mainly in the axial direction. At its top end, it reaches quasi a 1 cm thickness whereas the vapour layer just below is composed of relatively smaller quasi spherical bubbles (like on the (e) picture). A few tenths of second after \( t_{ONB} \), the wall is covered by a population of tiny bubbles (1 mm). This corresponds to times for which the wall temperature is stabilized. This flow pattern will be recovered during the next seconds also and corresponds thus to the steady configuration. Let us also remark that almost no bubble exists far from the wall, that is typical from such convective sub-cooled boiling case.

### 3.3. Localized first nucleation event

The wall temperature evolution reported in Fig. 6 corresponds to the location where the first temperature maxima is reached. This location coincides with the area outlined in red on picture (a) of Fig. 7 which correspond to the first bubble. It can appear anywhere around the semi-circular heated surface. In this case, the first bubble is nucleated on the front part of the foil (marked with a red zone). It then propagates around and along the heated foil. The time \( t_{ONB} \), deduced from the high-speed camera, corresponds to the black point on the temperature evolution: it is very close to the time for maximal temperature. The apparition of the first vapor bubble coincides in space and time with the first temperature decrease over the test section.

This correspondence is common to all the 50 tests where those events occur in the scope of both cameras. The value \( t_{ONB} \) of the temperature at the location of the first event and at the time \( t_{ONB} \) has been collected for several test sections and flow conditions. The values are always close to the local maximum at this location. They are reported on Fig. 8 and are slightly in the range \( 60 \degree C : 80 \degree C \). This value is compared to the theoretical temperature for transient convection at the same time \( t_{ONB} \) as given by the Eq. (5) validated on our study of this regime. On Fig. 6, it corresponds to the yellow diamond that slightly over-predicts the maximum value. For the set of tests considered, it is shown in Fig. 8 that this theoretical prediction is in a rather good agreement with experimental measurements, with a small tendency to over-predict the measured temperature with the model. Therefore, at first order, the temporal evolution of wall temperature at the location where nucleation will first take place is the one of transient convection until this time. No sign of any precursor event seems to be deducted from our thermal measurements.

The measurement of \( T_{ONB,exp} \) is made by the infra-red camera with an error of approximately \( \pm 0.1 \degree C \). The error bar corresponds to the symbol size.

### 3.4. Temperature at nucleation event and cavity size

The theoretical equilibrium superheat of a radius vapour bubble \( r_e \) can be calculated from Laplace and Clapeyron equations:

\[
\Delta T_e(r_e) = T_e(r_e) - T_{sat} = \frac{2\sigma T_{sat}}{\rho_v h_{fg} r_e}\tag{7}
\]

For a bubble in a cavity of size \( r_c \), Hsu [14] advises to take \( r_e = \frac{2}{5} r_c \). From the experimental values of \( \Delta T_{ONB} \) and Eq. (7), the cavity sizes on the metal foil that would correspond to the observed onset are about 0.11–0.15 \( \mu m \). Microscope and AFM visualisations showed that the heated foils have lamination grooves 1–10 \( \mu m \) large and 0.1–0.2 \( \mu m \) depth, with surface cavities from 50 nm to 0.2 \( \mu m \). The contact angle of the HFE7000 on the metal
foil has been measured of about 13° with a tensiometer DSA100. Big cavities, that would require low wall superheat to be nucleation sites are easily flooded, that inhibits nucleation. Therefore, nucleation is more likely to occur for high superheat temperatures, corresponding to small cavities with rc = 0.11–0.15 μm.

Hsu’s model takes into account the growth of the thermal boundary layer in the liquid: the nucleation occurs only when the liquid at the top of the bubble (at r = 2r_c) is at the equilibrium temperature calculated with Eq. (7). Berthoud et al. [15] and Su et al. [11] suggested and used this model to calculate the onset of nucleate boiling for transient heatings. Assuming a linear profile through the thermal boundary layer, the first vapour bubble superheat can be written:

$$\Delta T_{ONB} = \Delta T_{eq}(r_c) + \frac{2r_c}{\delta_{ONB}} (T_{eq} - T_b)$$

(8)

This equation shows that the wall temperature at nucleation is the sum of the theoretical equilibrium temperature in the homogenous case plus the thermal gradient across the bubble of size 2r_c. This second term introduces an impact of the wall heating rate on the nucleation temperature. It also depends on the cavity (and therefore on the bubble) size: the smaller the cavity size, the closer the nucleation temperature to the equilibrium one.

According to the Section 2.2, the evolution of the temperature and the thermal boundary layer thickness are self-similar during forced convection. Therefore, Eq. (8) can be written:

$$\Delta T_{ONB} = \Delta T_{eq}(r_c) + \frac{2r_c}{\delta_{ONB}} (T_{stat} - T_b)$$

(9)

$$\approx \Delta T_{eq}(r_c) + 2r_c \frac{\theta_{gen}}{\delta_c}$$

(10)

In this last equation, the steady thermal boundary layer thickness is approximated by δ_{hstat} ≈ δ_c/δ_{stat}. Eq. (10) is plotted on the left hand side graph of Fig. 9 with a dashed line for different r_c. The second term of Eq. (10) varies from 0.1 to 0.2 K in the experiments: the onset of boiling superheat appears to be nearly constant for a given cavity size and equal to the equilibrium superheat.

Su et al. [11] study transient ONB with an exponential heating with a characteristic time λ and their surface has small cavity sizes in comparison to the thermal boundary layer thickness. They show that ΔT_{ONB} can be well estimated with:

$$\Delta T_{ONB} = \Delta T_{eq}(r_c) + \frac{L}{\delta_c} (\Delta T_{eq}(r_c) + \Delta T_{sub})$$

(11)

with δ_c = 4a/λ for pool boiling (conduction heat transfer in the liquid) and δ_c = δ_{hstat} for dominant convective boiling. Eqs. (11) and (8) are very similar; however, in Su et al.’s study, the convective characteristic time is very small (maximum 110 ms) and they can consider an established thermal boundary layer when the nucleation begins.

Using Eq. (5) from 2.2 and Eq. (10), the first vapour bubble time can be calculated by:

$$t_{ONB} \approx -\frac{M_{ub}}{h_{stat}} \ln \left(1 - \frac{\Delta T_{eq} + \Delta T_{sub}}{\phi_{gen}} h_{stat} - 2r_c h_{stat} \right)$$

(12)

The first contribution in the logarithm corresponds to the time to increase the wall temperature to T_{eq} and the second contribution corresponds to the time to have the temperature T_{eq} at the top of the bubble, which is again negligible. Eq. (12) is plotted with a dashed line in the right hand side graph of the Fig. 9 and shows a rather good agreement with the experimental points. These experiments have been performed with three different test sections which could explain the dispersion of the results due to small difference in the surface state. The points above the dashed curves might correspond to smaller cavities.

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**Fig. 8.** Experimental value of the temperature at the first nucleation event T_{onb,exp} compared to the theoretical temperature for transient convection (Eq. (5)) at the same time T_{onb,th} for different test conditions. Flow rate corresponds to different colors: red: 0.11 s⁻¹, blue: 0.21 s⁻¹, green: 0.31 s⁻¹. Sub-cooling corresponds to different forms, □: ΔT = 13 °C, □: ΔT = 15 °C and ◇: ΔT = 17 °C. For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

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**Fig. 9.** Temperature and time of nucleation for different test conditions. Flow rate corresponds to different colors: red: 0.11 s⁻¹, blue: 0.21 s⁻¹, green: 0.31 s⁻¹. Sub-cooling corresponds to different forms, □: ΔT = 13 °C, □: ΔT = 15 °C and ◇: ΔT = 17 °C. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)
The superheat at the time of the nucleation event $\Delta T_{\text{ONB}} = T_{\text{ONB}} - T_{\text{sat}}$ has been plotted against the level of power intensity of the considered test $\phi_{\text{IN}}$ on Fig. 9. This wall superheat does not change much, neither with the heat flux, neither with the flow-rate, nor with the sub-cooling, and remains around 40 °C.

3.5. Delayed onset of boiling over the test section

In Fig. 10, the temporal evolution at different locations along the test section has been plotted on the same graph. They are indexed by the $Z$ variable that measures the vertical distance from the location of the first nucleation event $Z_{\text{ONB}} = 0$ cm that also corresponds to the first delay.

It can be seen that the time for the local maximum is all the more delayed with respect to $t_{\text{ONB}}$ that this distance is large. The delay is approximately 0.5 s for a 2 cm distance. This time scale is relatively of the same order of magnitude than the time scale for local relaxation from the maximum temperature to the steady value. We observe that such a delay is very reduced in the radial direction over the wall, in particular as soon as locations sufficiently far from the nucleation event are considered. Let us remark also that the temperature continues to notably increase after $t_{\text{ONB}}$ in the other locations than at the location of the event. Moreover, it can be seen a specific trend at the very last times of increase: the temperature increase rate seems to increase rather than decrease (the curve is rather convex than concave). After the decrease, all the temperatures converge toward approximately the same value around 50 °C. The overshoot of temperature depends therefore of the location considered. As a consequence, during the onset of the nucleate boiling regime, the deviation of temperature around a space average value (like the black curve on the graph) is relatively large. This leads to a difficulty in the interpretation of such averaged value in terms of nucleation mechanisms. The maximal value of the mean temperature is rather low with respect to local values and should be compared with caution with any model for nucleation. The typical relaxation time of the average temperature toward the steady value is clearly a combination of the local relaxation time that looks at first order very similar at different locations with the delayed decrease that looks like a front propagation.

3.6. Cooling at the onset of nucleate boiling

Let us focus on the local temperature decrease from the maximum temperature, say $T_{\text{max}}$, toward the steady nucleate boiling temperature, say $T_{\text{NB}}$. The difference between those two values is then referred to a transient overshoot $T_{\text{OV}} = T_{\text{max}} - T_{\text{NB}}$. The transient cooling is analysed locally for the location of the first nucleation event. The overshoot is therefore the minimum one with comparison to other locations for the same test. It has been plotted for different test conditions on the left hand side graph of Fig. 11. The overshoot order of magnitude is approximately tens of degrees but no clear tendency can be deduced and the dispersion is large. The time $t_{\text{OV}}$ between the maximal temperature and the first time it reaches the steady value $T_{\text{NB}}$ has been plotted on the right hand side of Fig. 11. The value is typically around 0.1 s with a rather small dispersion and no clear tendency with respect to the test conditions: liquid flow rate and sub-cooling.

The left hand side graph of Fig. 12 is a focus on the decrease phase of wall temperature at the nucleation site where the temperature time evolution has been reduced as $T' = (T - T_{\text{NB}})/(T_{\text{OV}} - T_{\text{NB}})$. The experimental measurement is clearly well fitted by an exponential law $T' = \exp(-t/t_{\text{OV}})$. For each test condition considered the value of the best fit for the parameter $t_{\text{OV}}$ has been reported on the right hand side graph of Fig. 12. The value is typically around 0.03 s with a rather low dispersion and no clear tendency with respect to the different test parameters.

It indicates that the cooling process during the transient establishment of nucleate boiling heat transfer at the location of the first nucleation event is very efficient (with a cooling rate of several hundreds of K s$^{-1}$). This cooling process seems insensitive to the flow and power conditions.

3.7. A vapor front propagation

For each pixel of the high-speed camera images, i.e. for each axial location along the wall, the vapor layer thickness $D_{b}[m]$ is the instantaneous lateral length corresponding to the number of pixels identified as being in vapor phase. This quantity can be associated with the size of the bubbles that can be seen on the pictures. The time and space evolution of the quantity $D_{b}$ is reported on the picture of Fig. 14a.

An algorithm allows to track the time at which a vapor layer appears. For this test, this first event is located at $Z = 3.07$ cm as represented by the grey circle. The white solid line joins the times of vapor apparition at each axial location $z$. It corresponds therefore to the boundary of non-zero vapor layer thickness above the wall. The vapor propagation is linear meaning the vapor layer progression has a constant axial velocity from its starting point at the first nucleation event, both downstream and upstream in this case. The white-dashed line corresponds to the maximum bubble height.

From the white lines slopes, the propagation speed of the vapor front along the vertical direction has been deduced for several test conditions. As shown on the Fig. 13, the velocity lies in the range [50 cm s$^{-1}$–100 cm s$^{-1}$] and is larger in the downstream/upward direction (positive velocity) than in the upstream/downward direction probably because of both the liquid flow and the buoyancy that should assist the vapour propagation in the upward direction.

Let us remark, that in some cases (more especially for the largest flow rates), there is no data for upstream propagation of the vapor front, since it does not propagate upstream from the nucleation point identified. The area can be kept without boiling for a while. Possibly, another nucleation event occurs downstream and nucleate boiling regime propagates toward the region.

During its axial progression downstream (upward), the vapor front has an increasing thickness until an approximately 7 mm extent (dark red zone for $Z < 1$ cm and $t \approx 0.1$ s). The time when $D_{b}$ first decreases corresponds to the tail of the vapor pocket. Its
trajectory (location of local $D_b$ maximum) has been determined thanks to an algorithm and is plotted as the white dashed line (the rightmost line) on Fig. 14.a. This line is approximately parallel with the apparition of the vapor (white solid line) with a delay of approximately 0.02 s.

Other relatively large vapor pockets growing along the wall can be detected afterwards (see the light green area parallel to the white line). They can be seen until approximately 0.15 s and their size is approximately 3 mm. It still corresponds to the transient period of nucleate boiling regime establishment. They could be associated with other nucleation events downstream that could initiate other large vapor pockets, but this is not evident to be conclusive on this behaviour.

After $t = 0.15$ s, $D_b$ decreases to approximately 1 mm, that corresponds to the size of the tiny bubbles in the steady sub-cooled nucleate boiling process.

### 3.8. Thermal analysis of the transition toward nucleate boiling

The wall temperature as a function of time and space is plotted in the Fig. 14b.

Temperature is relatively homogeneous in space during the first 0.05 s and after 0.15 s where it reaches a notably steady lower value. Let us focus on the transition zone between these two regimes. The lines deduced from the vapor front thickness analysis have been reproduced. It can be clearly seen that the wall

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Fig. 11. Overshoot: temperature difference and typical time for temperature decrease. Flow rate corresponds to different colors. red: 0.1 l s$^{-1}$, blue: 0.2 l s$^{-1}$, green: 0.3 l s$^{-1}$. Sub-cooling corresponds to different forms, $\Delta T = 13$ °C, $\Delta T = 15$ °C and $\Delta T = 17$ °C. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

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Fig. 12. Exponential model for the cooling after the overshoot and determination of an overshoot characteristic time.

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Fig. 13. Axial propagation velocity of the vapor front. Flow rate corresponds to different colors. red: 0.1 l s$^{-1}$, blue: 0.2 l s$^{-1}$, green: 0.3 l s$^{-1}$. Sub-cooling corresponds to different forms, $\Delta T = 13$ °C, $\Delta T = 15$ °C and $\Delta T = 17$ °C. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)
temperature continues its increase at the time (white lines) when the vapor front covers a specific location. The location of the maximum of temperature seems to be more correlated with the white dashed line that corresponds to the tail of the first vapor pocket.

The wall to fluid heat flux, as deduced from Eq. (1), is plotted for the same case on the right hand side of Fig. 14c. The lines deduced from the vapor front thickness analysis have also been reproduced. The first convection phase corresponds to rather low values for the heat flux. The last steady phase corresponds to the equilibrium between the generated heat flux $\phi_{\text{gen}}$ and the wall to fluid heat flux $\phi_w$. The largest heat flux values are clearly associated with the white dashed line and could reach up to $4 \times 10^5$ W m$^{-2}$ values. This is fully consistent with the evolution of wall temperature (from which it is partly deduced). It is worth noting that those local heat flux values are very large in comparison with the order of magnitude of the critical heat flux that is close to $10^3$ W m$^{-2}$ in similar conditions (from our own experiments).

Fig. 16a represents the logarithm of the ratio $\phi_w/\phi_{\text{gen}}$ of the same test. Once again, the black lines deduced from the analysis of the vapor front thickness analysis have been reproduced. It is very close to 0 (i.e. $\phi_w = \phi_{\text{gen}}$) as soon as the steady nucleate boiling regime is reached. During the transient convection stage, it indicates that the heat flux is approximately one order of magnitude less than the power intensity. The boundary of this regime is a short period represented by a rather thin orange line near the black dashed line. The heat flux is for a small fraction of time of the magnitude or larger than the power intensity. Despite this very evanescent step, the transition between those regimes is clearly made of two successive steps. The first one occurs when the first big vapor pocket covers the wall, i.e. between the black solid and the black dashed lines. It corresponds to a quasi-null heat flux toward the fluid (until around 1000 times less than the power dissipated). This corresponds clearly to the inflexion of the wall temperature just before the decrease that has been identified on the temporal local evolution of the wall temperature in Section 3.5. It is followed by a very rapid increase of the wall to fluid heat flux with maximal values more than 10 times the power dissipated. The transient heat flux during this transition toward nucleate boiling regime is therefore a very efficient heat transfer.
A possible interpretation of this behaviour is therefore as follows. Below the big vapor pocket that covers the wall following a first nucleation event, the heat flux is hindered. Due to the very low values of the wall to fluid heat flux, a transient dry-out of the wall can not be excluded. But this could also been explained by the fact that the vapor pocket insulated the wall from the rest of the flow and thereby of the efficiency of the coolant flow. When the pocket leaves the wall, the wall to fluid heat flux is suddenly very high: that could correspond to either the rewetting of the wall and intense vaporisation, or by the appearance of small bubbles in the tail of the large vapour bubble.

3.9. Local boiling curves

On Fig. 15, the local wall to fluid heat flux \( \phi_w \) as a function of the local wall temperature has been plotted at different axial elevations. The transient evolution of \( \phi_{gen} \) has also been represented by the red curve. Those elevations correspond to an horizontal line on the flux map. The fourth one corresponds to the elevation at which the first nucleation event occurs. Arrows on this curve indicate the time direction. Each curve, that can be associated to a more standard boiling curve, has been divided in three phases: in blue, the transient convection where the heat flux is always lower than the generated heat flux \( \phi_{gen} \); in dark green, the transition toward nucleate boiling regime and in purple the steady nucleate boiling regime where the mean heat flux equals \( \phi_{gen} \).

At the very end of the transient convection phase (i.e. in the blue part close to the maximal temperature), it can be seen on the top elevations that the heat flux tends to zero before increasing steeply. Then, the transition toward nucleate boiling regime occurs and the local heat flux reaches high values (approximately \( 3 \times 10^5 \text{ W m}^{-2} \)) almost all the time for temperature decrease. The evolution is rather similar between all locations. In some cases, the heat flux can temporarily reach zero values during the transition. It is associated to the trajectory of large vapor pockets (possibly other nucleation events) flowing from upstream and that could disturb the effective cooling process, eventually inducing local dry-out of the wall.

The mean boiling curve (the black line in the figure) has a reduced amplitude during the Overshoot and can not transcribe a local flux drops near the ONB. The classic approach of representing the boiling curve with a space averaged heat flux can not follow all the process during the onset of boiling that are mostly local and there is a lack of information with this representation. An additional approach is now provided to study this transition toward the FDNB.

3.10. Impact of test parameters on the behaviour

For a same sub-cooling and for 3 different flow rate values, the level of power has been varied as illustrated by the reduced wall to fluid heat flux space and time variation on Fig. 16. It shows that the behaviour is very similar for the different test conditions. The degradation of the wall to fluid heat flux (blue part) before the transition toward nucleate boiling is not seen in some high flow rate and relatively low power cases (d,g,h). In those latter cases, it can be seen on the high speed camera images, that the vapor pocket incoming from the nucleation site is not as large as in the other cases. This could be interpreted by the lack of any dry-out and therefore no heat transfer degradation. In some cases, it is seen that the wall upstream a nucleation site can be heated up during a relatively long time until another nucleation event leads to its cooling (like in the bottom part (\( z > 4 \text{ cm} \)) of cases d or f). In those cases, several successive events of heat transfer degradation and front propagation can be identified. From a more general point of view, the onset of nucleate boiling is all the more delayed than

![Fig. 15. Local boiling curves at different elevations.](image)
the flow rate is high. In some cases (g on the figure) the nucleation event occurs below (upstream) the frame of the IR camera.

4. Conclusions

An experimental study of the onset of convective nucleate boiling in transient conditions was performed in a geometry similar to a nuclear fuel rod surrounded by coolant. The flow Reynolds numbers studied varied from 14,000 to 52,000 and the sub-cooling from 5 to 20 K. The transient heating was achieved imposing heat flux steps from 20 to 500 kW m$^{-2}$, corresponding to heating rates from 10 to 500 K s$^{-1}$. Infra-red thermal measurements and high-speed camera visualizations have been synchronized in space and time and original algorithms of image processing have been developed. It brings more knowledge on the detailed processes along the wall during the onset of nucleate boiling. Models for the transient mechanisms have been proposed that will help better understanding of the phenomena occurring during a reactivity initiated accident in a pressurized water reactors.

The main findings of the study are:

- The evolution of the wall temperature and the evolution of the thermal boundary layer thickness are self-similar during the forced convection regime. Thus, the characteristic time to establish the wall temperature and the thermal boundary layer thickness is equal to the thermal mass of the wall over the steady convective heat transfer coefficient. It is important to take into account the thermal mass of the paint used to perform the infra-red thermal measurements. From the comparison between different characteristic time, we conclude that a quasi-steady model can predict well the temperature evolution during this regime.

- For the process of boiling onset, it has been shown that it is mostly driven by localized nucleation events followed by propagation mainly in the flow direction. Therefore space averaged analysis of the process is not well suited and leads to artificial smoothing of the local time evolutions (in temperature or in heat flux).
Conflict of interest

None.

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Appendix A. Supplementary material

Supplementary data associated with this article can be found, in the online version, at https://doi.org/10.1016/j.ijheatmasstransfer.2019.04.069.

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