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Thermoelectric performance of a material is determined using a figure of merit (FOM) determined as $ZT = \sigma S^2 T/\kappa$ where $\sigma$ is the electrical conductivity, $S$ is the Seebeck coefficient, $\kappa$ is the thermal conductivity, and $T$ is the temperature). In the case of a thin film, it is normal in the first approach to consider calculating the FOM by using the thermal conductivity of the film. However, both the thermal influence of the substrate and the emissivity of the film must also be taken into account. In the present work, the heat transfer model is used in order to study the influence of the thermal conductivity, the thickness, and the emissivity of the film on the thermal gradient of the stack (substrate + thin film). The limits of these three parameters are determined in order to have the temperature variation due to the presence of the film compared to the substrate alone that remains less than 1%. Under these limits, the thermal conductivity of the substrate can be taken into account instead of the thermal conductivity of the thin film, and a modified FOM ($Z'T$) can be calculated. The present study leads to the determination of the validity of modified ZT. In the case of CuCrO$_2$:Mg thin films, the model shows that the use of $Z'T$ is valid. The calculated value of $Z'T$ with the measured Seebeck coefficient and the electrical conductivity as a function of the temperature for 100 nm thick films and the temperature dependent thermal conductivity taken from the literature reached 0.02 at 210 °C. 

A thermoelectric module made with this material showed 10.6 nW when 220 °C is applied at the hot side. 

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I. INTRODUCTION

Among the physical properties of materials, knowledge of the thermal properties is crucial for a large range of applications such as microelectronics, microelectromechanical system, thermal barriers, thermoelectrics, and photonics. The determination of thermal conductivity is especially important to calculate the figure of merit $ZT = \sigma S^2 T/\kappa$ which can reveal the performance of a thermoelectric material. The measurement of the thermal conductivity is fairly well controlled in the case of bulk materials despite the long measurement time, the cost, the specific size of the sample, and the specimen preparation. However, it is even harder to determine the thermal conductivity in the case of thin films due to the small quantity of matter, which transfer the heat. The 3ω method which is generally used to characterize the thermal conductivity of the thin film, requires some approximations as isothermal and quasi-static substrate, 1D quasi-static heat flow in the film, negligible convection and radiation, and insulating thin film. This method is restrictive due to the use of microelectronic processes with several steps, and it is not valid for samples with high porosity.

In a previous work, we have studied the thermoelectric properties of Mg doped CuCrO$_2$ thin films, deposited using radio frequency magnetron sputtering. We have optimized the annealing temperature and the thickness in order to get the highest power factor (PF = $S\sigma$). One advantage of the thin films as thermoelectric materials is that the thermal conductivity can be lower compared to the bulk due to microstructural effects. Nevertheless, due to the difficulty of the thermal conductivity measurement on thin films, the figure of merit $ZT$ could not be calculated. Some authors took into account the contribution of the substrate in the $ZT$ determination. Pérez-Rivero et al. have calculated a modified figure of merit, $Z'T$, using only the thermal conductivity of the substrate without any demonstration of the validity of this relation.

In the specific case of a thin film, one can expect that the temperature gradient in the thin film deposited on the substrate can be influenced by the thermal conductivity of the substrate. In this work, we have focused on the contribution of the substrate thermal properties on the thermal behavior of the film. The impact of different characteristics of the film such as the emissivity, the thermal conductivity, and the thickness on temperature gradient at the surface of the thin film have been checked.

II. METHODOLOGY

A. Description of the model geometry

In this work, Comsol Multiphysics software is used in order to study the thermal properties of a thin film deposited on a substrate. The studied geometry is based on a 3D model of the substrate and the film as its top surface (Fig. 1). Fused
silica and Mg doped CuCrO₂ are assigned for the substrate and the film, respectively.

In order to study the heat transfer and determine a temperature profile, four measuring points are placed at the surface of the thin film and at the surface of the substrate without film to record the temperatures. Then the physical “heat transfer in solids” is applied. This physical requires several physical properties (emissivity, specific heat, thermal conductivity, and heat exchange coefficient), initial conditions (heat source temperature and environmental temperature), and boundary conditions (thicknesses and dimensions) which will be described in the next part. Following this, the mesh is selected. The tetrahedral elements with fine mesh are well adapted for this model and are geometrically simple. Indeed, the type of the mesh can strongly affect the simulation so the elements and element size were carefully chosen. Once the mesh is correctly made and the mesh nodes coincide with the measurement points, the study is carried out in a steady state.

B. Description of the used heat transfer laws

The heat transfer in the solid model uses the heat Eq. (1) as the mathematical model and can be characterized by three mechanisms described in Fig. 2.

\[
\rho C_p \frac{\partial T}{\partial t} + \Delta \mathbf{q} = Q,
\]  

where \( \rho, C_p, T, t, q, \) and \( Q \) are the density, the heat capacity, the temperature, the time, the heat flux by conduction, and the heat source, respectively. The heat source describes heat generation within the domain.

In this study, the temperature of the heat source is fixed to 100 °C, and the contact thermal resistance between the substrate and the film is neglected because the CuCrO₂:Mg thin film is dense and well attached to the substrate.²³

For a steady-state problem, the temperature does not vary with time and the first term disappears.

Figure 2 describes the heat transfer model where three modes (heat conduction, heat convection, and radiation) exist.

- The heat conduction in solids is the transfer of heat occurring by free carrier motion and lattice/molecule vibration. In general, the main part of the heat transfer in solids is due to the heat conduction which is described by Fourier’s law¹⁸ in Eq. (2),

\[
\mathbf{q} = -k \Delta T,
\]  

where \( \mathbf{q} \) is the heat flux vector, \( k \) is the thermal conductivity that is taken as isotropic in this study, and \( \Delta T \) is the temperature gradient.

- The heat convection occurs when the heat is dissipated due to a flowing fluid.¹⁹ The heat dissipation from a solid surface to a fluid is described by the heat transfer coefficient, \( h \), following Eq. (3).

\[
\mathbf{n} \cdot \mathbf{q} = h (T - T_m),
\]  

where \( \mathbf{n} \) is the normal vector of the boundary and \( T_m \) is the room temperature.

In our case, the external natural convection with a laminar airflow²⁰ already implemented in Comsol is chosen.

- The heat transfer by radiation takes place through the photons at the surface of the material and describes Stefan Boltzmann’s law.

\[
\mathbf{n} \cdot \mathbf{q} = \varepsilon \sigma (T^4 - T_m^4),
\]  

where \( \varepsilon \) is the emissivity and \( \sigma \) is the Stefan’s constant (5.67 × 10⁻⁸ W m⁻² K⁻⁴).

III. EXPERIMENTAL DETERMINATION OF THE PHYSICAL PROPERTIES

In order to solve the above equations, some unknown properties such as the heat capacity, the emissivity, the density, and the thermal conductivity of the substrate and the thin film must be determined in advance.

There is no influence of specific heat capacity in the steady state study as shown in Eq. (1). However, we have still determined the value of the specific heat capacity using the Differential Scanning Calorimetry (DSC) model Mettler.
Toledo DSC 1 with HSS7 sensor. From the DSC signals, the specific heat capacity of the Mg doped CuCrO$_2$ powder is calculated\textsuperscript{21} as a function of the temperature. The obtained specific heat capacity is 53.6 J kg$^{-1}$ K$^{-1}$ at 100 °C. The heat capacity of the fused silica (730 J kg$^{-1}$ K$^{-1}$) is taken from the literature.\textsuperscript{22}

The emissivity of the samples (fused silica and CuCrO$_2$: Mg film on fused silica) is measured with an emissometer model AE1. This apparatus approximates total hemispherical emittance at 65 °C. Prior to the measurement, the calibration of the emissometer is done with a high emittance standard made of aluminum hard black anodized Teflon infused ($\varepsilon = 0.87$) and a low emittance standard with nickel-plated brass ($\varepsilon = 0.06$). Then the measurement gives 0.83 for the fused silica and 0.76 for the 300 nm thick CuCrO$_2$:Mg film on fused silica. The values of the emissivity are assumed constant when the temperature is increased. In order to check the influence of the substrate on the obtained emissivity value, the emissivity of several films with different thicknesses (100, 300, 600 nm) was measured and showed the same value. Therefore, CuCrO$_2$:Mg films are considered to be opaque for the infrared photons emitted by the substrate.

The density of fused silica and CuCrO$_2$ are taken, respectively, from Refs. \textsuperscript{22} and \textsuperscript{23} (2.21 g.cm$^{-3}$ and 5.49 g.cm$^{-3}$) and is supposed to be constant with the temperature. In the same way, the thermal conductivity of the substrate is obtained from Ref. \textsuperscript{24} (1.38 W m$^{-1}$ K$^{-1}$) at room temperature and does not vary a lot till 250 °C. Concerning the thermal conductivity, CuCrO$_2$ bulk is reported to have a value of 8 W m$^{-1}$ K$^{-1}$ at 300 K.\textsuperscript{25} In order to broaden the scope of the study, parameters such as the thermal conductivity, the thickness, and the emissivity of the film are varied in a wide range.

**IV. RESULTS AND DISCUSSION**

The temperatures at the surface of the film and at the surface of the substrate given by the simulation are used to calculate $\alpha$. The coefficient $\alpha$ shows the relation between the temperature difference at the surface of the substrate without film [$T_{source} - T_{n}^{s}$] and the temperature difference at the surface of the film deposited on the substrate [$T_{source} - T_{n}^{lm}$] for a given location. Figure 3 shows a schematic representation of the film deposited on the substrate and describes the zones where the temperature differences are taken by indicating an example with a measuring point 4. The definition of the coefficient $\alpha$ allows us to know how the presence of the film on the substrate influences the heat transfer. To facilitate the representation of the results, $(1 - \alpha)$ is taken instead of $\alpha$. If the value $(1 - \alpha)$ is positive ($0 < \alpha < 1$), the presence of the film boosts the heat transfer and increases the temperature at the surface of the film. If the value $(1 - \alpha)$ is negative ($\alpha > 1$), the presence of the film decreases the temperature at the surface of the film. Finally, if the value $(1 - \alpha)$ is equal to 0 ($\alpha = 1$), the presence of the film does not influence the temperature and is equal to the temperature of the substrate (without film) at the given location.

$$\alpha = \frac{(T_{source} - T_{n})^{lm}}{(T_{source} - T_{n})^{s}}.$$  

(5)

The factor of merit $ZT$ of a material is calculated by using the below relation,

$$ZT = \frac{\sigma S^2}{k} T,$$  

(6)

where $\sigma$ is the electrical conductivity, $S$ is the Seebeck coefficient, $k$ is the thermal conductivity, and $T$ is the temperature.

Regarding thermoelectric thin film, it is the thermal conductivity of the layer ($k = k_{\ell}$) which is taken into account for the calculation of $ZT$. However, in this case, the influence of the substrate is totally neglected. On the contrary, some authors\textsuperscript{17} use the thermal conductivity of the substrate ($k_{s}$) for the calculation of a modified $ZT$ which

![FIG. 3. Schematic representation of the film deposited on the substrate.](image)

**FIG. 4.** (a) Evolution of $(1 - \alpha)$ as a function of the film thermal conductivity. (b) $k_{\ell}$ limit as a function of the distance between the source and the measuring points.
can be defined as

\[ (Z') = \frac{\sigma S^2}{k_b} T. \]  

(7)

The aim of the present work is to study the influence of three parameters (the thermal conductivity, the thickness, and the emissivity of the film) on the validity limit of the modified figure of merit \((Z' T)\) of the block (substrate + film). The condition for the determination of the limit is fixed at 1% of temperature variation due to the presence of the film at the surface compared to the temperature at the surface of the substrate without the film. In other words, this corresponds to 

\[(1 - \alpha) < 0.01.\]

### A. Influence of the thin film thermal conductivity

Figure 4(a) shows the evolution of \((1 - \alpha)\) as a function of the film thermal conductivity when other properties are fixed with the values exposed in Table I. The film thermal conductivity is varied from 0.5 to 1000 W m\(^{-1}\) K\(^{-1}\). In this range, the obtained values of \((1 - \alpha)\) are positives for the four different measuring points which indicates that the presence of 300 nm film increases the temperature at the surface compared to the substrate only. This temperature increase is more and more important when the conductivity of the thin film increases. Obviously, it also depends on the measuring points. The variation of \((1 - \alpha)\) below 1.38 W m\(^{-1}\) K\(^{-1}\), which corresponds to the thermal conductivity of the substrate (fused silica), is not obvious. In fact, the predictable trend is an evolution of \((1 - \alpha)\) under 0 when the film thermal conductivity is lower than the substrate thermal conductivity. The present variation of \((1 - \alpha)\) indicates that even if the main part of the heat transfer in solids is due to the heat conduction, the other type of heat transfers (convection and radiation) still occurs. As the heat convection is assumed the same in the case of the substrate only and the film deposited on the substrate, and as the geometry does not change, the emissivity is the second main part of the heat transfer, which must not be neglected.

The 1% increase of \((1 - \alpha)\) due to the presence of the film is given with the film thermal conductivity limit extracted from Fig. 4(a). This film thermal conductivity limit is plotted as a function of the distance between the heat source and the measuring points for different heat source temperatures in Fig. 4(b). Below this limit (hatched area), the temperature at the surface of the film is assumed to be the same as the temperature at the surface of the substrate without film when the same heat temperature is applied at the edge. The results show that the film thermal conductivity limit increases with the distance between source and measuring point and with increasing heat source temperature. It indicates that in general the longer the length of the thermoelectric leg, the higher the limit of the film thermal conductivity. It is also true for the high temperature source. Besides, CuCrO\(_2\) bulk is reported to have a thermal conductivity of 8 W m\(^{-1}\) K\(^{-1}\) at 300 K\(^{25}\) and 7 W m\(^{-1}\) K\(^{-1}\) at 300 K\(^{26}\) in Mg doped CuCrO\(_2\) bulk, and it is quasi constant with increasing temperature. In our case, the film thermal conductivity must be higher than 100 W m\(^{-1}\) K\(^{-1}\) to have an effect on the temperature difference when the length of thermoelectric leg exceeds 10 mm.

### B. Influence of the thin film thickness

The thin film thickness is an important parameter that influences the heat transfer in solids. Figure 5(a) shows the film thickness limit as a function of the distance between the source and the measuring points for three films’ thermal conductivities. For a given film thermal conductivity, the thickness limit increases when the distance between the source and the measuring points increases. For instance, 100 nm thick film is in the domain where \((1 - \alpha)\) is under 1% even when the film thermal conductivity is 100 W m\(^{-1}\) K\(^{-1}\).

Figure 5(b) shows the film thickness limit as a function of the film thermal conductivity for two different heat source temperatures.

### Table I. Properties of the CuCrO\(_2\) and the fused silica used in the model.

<table>
<thead>
<tr>
<th>Physical properties</th>
<th>CuCrO(_2)</th>
<th>Fused silica</th>
</tr>
</thead>
<tbody>
<tr>
<td>Specific heat capacity (C(_p)) at 100 °C</td>
<td>536 J kg(^{-1}) K(^{-1}) (determined on powder)</td>
<td>730 J kg(^{-1}) K(^{-1})</td>
</tr>
<tr>
<td>Density (ρ)</td>
<td>5.49 g cm(^{-3})</td>
<td>2.21 g cm(^{-3})</td>
</tr>
<tr>
<td>Thermal conductivity (k) at 300 K</td>
<td>8 W m(^{-1}) K(^{-1}) (reported for bulk)</td>
<td>1.38 W m(^{-1}) K(^{-1})</td>
</tr>
<tr>
<td>Emissivity (ε)</td>
<td>0.76 (measured on 1 mm thick fused silica)</td>
<td>0.83 (measured on 1 mm thick fused silica)</td>
</tr>
</tbody>
</table>

*Reference 22.
*Reference 23.
*Reference 25.
*Reference 24.
temperatures at point 4 (d_{source-measuring point} = 20 mm). The tendency is similar for the whole measuring points (points 1 to 3 not shown here). The thickness limit decreases when the film thermal conductivity increases. It reveals that the thinner a film is, the higher its thermal conductivity can be without significant consequences on the temperature gradient. The knowledge of the CuCrO$_2$:Mg bulk thermal conductivity (7 W m$^{-1}$ K$^{-1}$ at 300 K$^{26}$) gives an approximate film thickness limit of 10 μm when the measuring point is taken at 20 mm from the heat source. Consequently, working with a few hundred nanometers thick film allows neglecting the thermal conductivity of the film and using the modified factor of merit (Z’T) with the thermal conductivity of the substrate. It also enables to use a high thermal conducting material without any influence on the temperature gradient.

C. Influence of the emissivity

It is necessary to know the impact of the film emissivity on the temperature gradient at the surface of the film. Emissivity reflects the ability of the material to lose heat by radiation. The emissivity taken by a material ranges from 0 to 1. Although the emissivity is an intrinsic property of a material, it can be increased by adjusting the geometry, resulting to an effective emissivity, which can be greater than 1 in the case of a very rough system. In the case of this simulation, the geometry is plane and does not take into account the roughness, so that the emissivity is limited to the value of 1. At a given measuring point, it is possible to define an emissivity range of the film (ε_f) within which the temperature difference between the deposited film ($T_f$ + ε_f) and the single substrate ($T_s$) is less than 1%.

Figure 6(a) shows this emissivity range of the film (colored zone) as a function of the distance from the source for three different values of the substrate thermal conductivity. The temperature source is fixed at 100 °C. The ranges are bordered by the emissivity limit values for which the temperature variation of the film relative to the single substrate is 1%. The values below the low limit of ε_f correspond to the emissivities for which the temperature of the film will be greater than the substrate ($T_f$ + ε_f > $T_s$) with a difference more than 1%. On the contrary, the values above the upper limit of ε_f correspond to the emissivities for which the film temperature will be lower than the substrate ($T_f$ + ε_f < $T_s$) with a difference more than 1%. In that case, the upper limit is only visible for small distances, less than 10 mm from the source, and for films with low thermal conductivity. For longer distances and higher thermal conductivities of the film, the high limit would correspond to values of ε_f greater than 1, which is outside the limit fixed in the previous paragraph. Even with high emissivity, it is not possible to obtain thin film temperature lower than the substrate alone if the film is thermally too conductive or if the measuring point is too far from the source. It can be seen in Fig. 6(a) that whatever the thermal conductivity, the emissivity range allowed to have less than 1% temperature differences widens with the distance from the source. From these results, it can be concluded that (Z’T) can be used for 300 nm thick CuCrO$_2$:Mg thin films which have an emissivity and a bulk thermal conductivity of 0.76 and 7 W m$^{-1}$ K$^{-1}$, respectively.

In Fig. 6(b), it is observed that when the thermal conductivity of the film increases, the emissivity limit shifts to higher values but it is limited by the threshold value of 1 (as a result, the range of allowed emissivity values is reduced). Figure 6(b) also shows that the allowed emissivity range increases with increasing temperature of the source. Thus, when the temperature of the source is high, it is possible to use a less emissive film without affecting the temperature gradient.

Figure 7 represents the evolution of the emissivity needed in order to have no difference in temperature between the deposited film and the substrate without film (1 − α = 0).

FIG. 6. (a) The emissivity limit as a function of the distance between the source and the measuring points for three film thermal conductivities. (b) The emissivity limit as a function of the film thermal conductivity for two different heat source temperatures at point 4.

FIG. 7. The emissivity for (1 − α = 0) as a function of the film thermal conductivity.
Our simulations have shown that this emissivity value is independent of the distance from the source and the temperature of the source. Figure 7 shows that when the thermal conductivity of the film increases, it is necessary to increase its emissivity as well.

In conclusion, we note that just like the thermal conductivity and the thickness of the film, emissivity plays an important role in the case of thin films thermal gradient. However, it is rarely taken into account for thermoelectric applications. In fact, when it is high, it allows obtaining higher temperature gradients that is beneficial for thermoelectric applications.

D. Experimental results

The simulation results have shown that the modified ZT can be used in the case of the CuCrO$_2$:Mg thin films. In Fig. 8, (Z'T) of 100 nm thick CuCrO$_2$:Mg films is plotted as a function of the temperature compared with the data from the literature. The values of the modified ZT are calculated using the measured Seebeck coefficient and the electrical conductivity as a function of the temperature (from 40 to 210 °C) published in our previous work\cite{21} and the temperature dependent thermal conductivity of the fused silica published by Combis et al.\cite{24} Thanks to the thermal properties of the CuCrO$_2$:Mg film, (Z'T) attained $2 \times 10^{-2}$ at 210 °C, whereas CuCrO$_2$:Mg bulk studied by Hayashi et al.\cite{25} reached only 0.008 at the equivalent temperature. Pérez-Rivero et al.\cite{13} published a Z'T of $7 \times 10^{-3}$ at 180 °C in the case Ca$_3$Co$_4$O$_9$ epitaxial thin film on yttria stabilized zirconia crystalline substrate. In comparison, the value of (Z'T) of delafossite thin film is higher due to a higher Seebeck coefficient of CuCrO$_2$:Mg and a lower thermal conductivity of the fused silica substrate. This result shows clearly the advantage of working with CuCrO$_2$:Mg film compared to the bulk in terms of ZT.

Due to the interesting thermoelectric performance of the 100 nm thick CuCrO$_2$:Mg film, we decided to elaborate a thermoelectric module made with three legs of CuCrO$_2$:Mg film. The legs were connected with a gold layer. In order to characterize this module, one side of the module was heated and the other side was left untouched under air as shown in the inset of Fig. 9(a). The applied temperature at the hot side and the measured temperature at the cold side of the module were plotted in Fig. 9(a). The cold side temperature was measured using an infrared camera and carbon spots with an emissivity of 1 were used for the temperature determination. The slight variation of the temperature at the cold side from 22 °C to 46 °C when the hot side temperature was increased from 25 °C to 220 °C indicated once again a low thermal conductivity of the CuCrO$_2$:Mg film and gave a high temperature gradient, benefit for thermoelectric applications. Figure 9(b) shows the maximum electrical power generated by the three legs thermoelectric module when the hot side temperature is increased. It reached 10.6 nW when 220 °C is applied at the hot side. Saini et al.\cite{22} have also elaborated a thermoelectric module with oxides films (Ca$_3$Co$_4$O$_9$ as p type and ZnO:Al as n type) deposited on fused silica and reported 0.34 pW when 300 °C is applied at the hot side. Compared to the literature, the present study showed an encouraging result for practical applications at high temperature.

V. CONCLUSIONS

In this article, the influence of the thermal conductivity, the thickness, and the emissivity on the heat transport of CuCrO$_2$:Mg film deposited on fused silica is studied using simulations. The results gave limit values from which the temperature increase due to the film is lower than 1% compared to the substrate only. For the thin films, which have the thermal conductivity, the thickness, and the emissivity value under the limit, the modified ZT can be used to determine the thermoelectric performance of the thin film. The simulation results also allowed revealing the importance of taking into account the emissivity in the ZT calculation which is rarely studied. In fact, by increasing the film emissivity
value, the stack (substrate and film) can be cooled down which is beneficial for thermoelectric properties of the material. Mg doped CuCrO$_2$ film is situated in the valid zone to use of the modified ZT. The calculated value of $(Z^\prime T)$ reached 0.02 at 210 °C which encouraged the elaboration of the thermoelectric module based on this material. The characterization of the module revealed a maximum power of 10.6 nW when 220 °C is applied at the hot side and the cold side is left untouched. This study showed interesting thermoelectric performances to a potential application of CuCrO$_2$:Mg films as a thermoelectric material at high temperature.