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Abstract - This paper presents a multi phase induction system modelling for a metal disc heating and further industrial applications such as hot strip mill. An original architecture, with three concentric inductors supplied by three resonant current inverters leads to a reduced element system, without any coupling transformers, phase loop, mobile screens or mobile magnetic cores as it could be found in classical solutions. A simulation model is built, based on simplified equivalent models of electric and thermal phenomena. It takes into account data extracted from Flux2D® finite element software, concerning the energy transfer between the inductor currents and the piece to be heated. It is implemented in a versatile software PSim, initially dedicated to power electronic. An optimization procedure calculates the optimal supply currents in the inverters in order to obtain a desired power density profile in the work piece. The paper deals with The simulated and experimental results are compared in open-loop and closed loop. The paper ends with a current control method which sets RMS inductor currents in continuous and digital conditions.

Index Terms – induction heating, metal industry, current control, electromagnetic induction, multi phase.

I. INTRODUCTION

Nowadays, induction heating systems are expanding in industry because of the induced advantages. High power density can be reached quickly with an increased flexibility and thanks to the associated power electronics, a fine control of the heat profile can be implemented. It is also a good solution when heating inaccessible parts of a piece is necessary [1][2]. This kind of heating is most often used in steel and metal working industries for heat treating, welding and melting, for drying, for merging and even in the food industry. But it also appears in degreasing, stripping, or galvanizing applications. Compared with convection or radiation ovens, this technique provides better performance for heating metal parts because the heat is generated directly inside the material. Moreover, the induction heating systems have better power/volume ratios and do not locally generate any kind of exhaust gases.

There are two general types of induction heating systems for strip heating, depending on the flux direction: transversal flux in Fig.1a or longitudinal flux in Fig. 1.b.

This work will only focus on high power density and multi phase systems for industry applications and on the first type of flux generation which is the most suitable for thin disc or strip heating. The future objective of this work is the dynamic control of high power (>1MW) induction systems for industrial applications such as metal strip heating in a hot strip mill.

Conventional control solutions for multi inductor systems [2][3][4] advocate the use of several inductors with mobile magnetic screens and mobile flux concentrators (Fig.2). The additional devices permit to apportion the magnetic fields produced and thus to adapt the system to different formats of material and changes in position in order to reach the desired temperature gradients. The processing lines are then subject to mechanical adjustments and/or maintenance as often as necessary to change the material to be heated. It is important to notice that without any model, the desired power profile is obtained by successive trail and error setting tests which are time consuming.

Fig. 1a : transverse flux inductor
Fig.1b : longitudinal flux inductor

Fig. 2 : transverse flux induction heating with moving parts
Numerous papers and patents have been published on the automatic control of single phase induction heating systems [5-9] but fewer on multi phase generators. Even in that particular case, they often present a rather complex solution with one dc/dc converter (or one rectifier) plus one resonant inverter per phase [10][11]. One solution [12] proposes to manually change the coil connection in order to adapt the generator to the load, while another implies some variable passive elements [13] or some decoupling transformers between the different phases [14] which are certainly bulky and costly. Parallel connection of serial resonant inverters behind only one rectifier is possible [15] but in rather high frequency and with additional serial inductances. A last, a reduced set of papers deal with the specific problem of multiphase electronic or digital current control [16-19].

In this work, a reduce element system is first proposed with several inductor coils in order to obtain flat power density and temperature profile in the stainless steel piece to be heated. The resulting high complexity, mainly due to interactions between the converter, the inductors and the heat piece, makes the modelling rather difficult. Nevertheless it is possible to separate the system into two parts [19] : on the one hand a power part, on the other hand a thermal part. Few software like Flux2D® allow magneto-thermal studies and their complexity and their long simulation time make them unsatisfying (long hours or days of simulation). To overcome these drawbacks, a simplified model of the complete system was developed, including control, power electronics, load thermal behaviour and power exchange between the supply and the loads. The whole model is presented with the comparison between open-loop and experimental results. In the last part, a simple current control is tested in digital conditions.

II. ELECTRICAL AND THERMAL MODEL

The reduced element system is composed by 3 inductor concentric coils arranged face to face in a transverse flux and a disk plate i.e. the load to be heated. Fig. 3 presents a simplified diagram of the coil/disc arrangement, while Fig 4. shows the exact concentric and face-to-face configuration. Each coil is supplied by a resonant inverter but with a common ac/dc rectifier + inductor as a controlled current source connected to the grid. The model can be divided into three parts: the electrical part with the inverters, capacitors and coupled inductors, the electrical/power part with a current/power transformation inside the load disc and the thermal part (Fig. 5).

The first one can be represented by four electrical circuits (one for each coil and the last for the material to be heated which is flowed by currents in short circuit with zero voltage) reduced to three relationships, presented in a matrix way in (1). The system can be described by an impedance matrix \( Z_{ij} \) linking the three inductor voltages \( V_1, V_2 \) and \( V_3 \) to the associated inductor currents \( I_1, I_2 \) and \( I_3 \) [19].

\[
\begin{bmatrix}
V_1 \\ V_2 \\ V_3
\end{bmatrix} =
\begin{bmatrix}
Z_{11} & Z_{12} & Z_{13} \\ Z_{21} & Z_{22} & Z_{23} \\ Z_{31} & Z_{32} & Z_{33}
\end{bmatrix}
\begin{bmatrix}
I_1 \\ I_2 \\ I_3
\end{bmatrix}
\]

(1)

\[
Z_{ii} = \left( R_i + \frac{\omega^2 M^2_i R_i}{R_i^2 + (\omega L_i)^2} \right) + j \omega \left( L_i + \frac{\omega^2 M^2_i L_i}{R_i^2 + (\omega L_i)^2} \right)
\]

(2)

\[
Z_{ij} = \left( \frac{\omega M_{ij} M_i R_j}{R_i^2 + (\omega L_i)^2} \right) + j \omega \left( M_{ij} + \frac{\omega M_{ij} L_i L_j}{R_i^2 + (\omega L_i)^2} \right)
\]

(3)

- \( R_i \) and \( L_i \): self resistances and inductances for inductor i
- \( M_{ij} \): mutual inductance between inductors i and j.
- \( M_{ii} \): mutual inductance between inductor i and the material,
- \( R_4 \) and \( L_4 \): stainless steel disc plate inductance and resistance

For the sake of convenience and time savings, the terms of the matrix are measured (4) using the “pseudo energy” method by measuring V and I, active and reactive power according to [22].

\[
\begin{bmatrix}
33,1 + j244,66 \\
25,96 + j43,77 \\
21,48 + j24,33
\end{bmatrix} \begin{bmatrix}
25,83 + j43,61 \\
67,31 + j247,32 \\
65,93 + j113,66
\end{bmatrix} \begin{bmatrix}
508,20 + j681,39 \\
107,11 + j568,20
\end{bmatrix}
\]

(4)

The supply part consists of three current inverters in series and a controlled current source as shown in Fig. 6. The inverter current namely \( I_{ic,1} \) and the inductor current \( I_1 \) waveforms are shown in Fig. 7 for the phase 1 for example. The quasi sinusoidal shape of the inductor current \( I_1 \) can be noticed, due to the high quality factor LC resonant circuit.

To obtain the inverter current waveforms, specific angles are calculated and transformed so as to give the correct switch orders. These angles are the result of an optimization procedure of the power density profile in the plate which is not detailed here but in [20].

Fig. 3. Coils and work piece schematic coupling

Fig. 4. Induction heating device coils, disc and bus-bar.
The second part is based on the calculation in Flux2D® of an image of the power density distribution created in the load. The relationship depicted by (5) gives the power density from the total induced current in the material.

\[ D_p(x_i) = \rho_{disc} J_{disc}(x_i) \]  \hspace{2cm} (5)

With:
- \( x_i \): abscissa of the thermocouple \( i \),
- \( J_{disc} \): total induced current in the material,
- \( \rho_{disc} \): resistivity of the material,
- \( D_p \): power density to the abscissa \( x_i \).

\( J_{disc} \) represents the total induced currents in the material at any point \( i \) along the radius when \( \rho_{disc} \) is the resistivity. This current density \( J_{disc} \) is based on image functions extracted from Flux2D® at each abscissa along the disc radius [19] as expressed in (6). Fig. 8 and Fig. 9 respectively show the real part and the imaginary parts of the functions induced by each of the 3 inductors when separately considered.

\[ J_{disc}(x_i) = \sum_{k=1}^{3} \left[ f_{kr}(x_i) \cdot I_{kr} - f_{kl}(x_i) \cdot I_{kl} \right] + j \sum_{k=1}^{3} \left[ f_{kr}(x_i) \cdot I_{kr} + f_{kl}(x_i) \cdot I_{kl} \right] \]  \hspace{2cm} (6)

where
- \( f_{kr}(x_i) \) is the real part of the image of induced distribution current to the abscissa \( x_i \),
- \( f_{kl}(x_i) \) is the imaginary part of the image of induced distribution current to the abscissa \( x_i \),
- \( I_{kr} \): real part of the current \( I_k \),
- \( I_{kl} \): imaginary part of the current \( I_k \).
Then, for the last part, the temperatures in the material derive from (7),

$$D_p(x_i) = \rho \cdot c \cdot \frac{d\theta_i}{dt} + \frac{2h}{e} (\theta_i - \theta_a) \quad (7)$$

considering

- $D_p(x_i)$: power density to the abscissa $x_i$,
- $\theta_i$: temperature of the disc to the abscissa $x_i$,
- $\theta_a$: ambient temperature,
- $\rho$: relative density,
- $c$: heat capacity of the material,
- $h$: convection coefficient,
- $e$: disc thickness.

One of the advantages of the multi-phase induction system is its flexibility, that is to say, its ability to face various power density profiles: linear or exponential, rising or downward as shown hereafter. The optimization procedure leads to the inductor currents which are necessary to obtain the corresponding temperature profiles inside the disc. Fig. 10 and 11 show the case of an exponential rising profile. The reference profile and the density calculated by the mathematical optimization procedure in a theoretical way, is plotted in Fig. 10. The corresponding simulation with power electronic supply and the results are shown in Fig. 11. It is easy to see that they are in good agreement.

In this first study, the aim is to obtain a flat temperature profile. Then, the developed optimization procedure [18][19] leads to the optimal inductor currents, i.e. amplitudes and phase shifts with respect to phase 1, which are listed in Table I.

### Table I

<table>
<thead>
<tr>
<th>Inductor currents</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Source current: $I_s = 87.9$ A</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Inductor</th>
<th>RMS values (A)</th>
<th>Phase shifts (°)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$I_1$</td>
<td>253.6</td>
<td></td>
</tr>
<tr>
<td>$I_2$</td>
<td>14.9</td>
<td>$\alpha_{21}$</td>
</tr>
<tr>
<td>$I_3$</td>
<td>93</td>
<td>$\alpha_{31}$</td>
</tr>
</tbody>
</table>

### III. Temperature Influence

The model parameters will change as the temperature increases. This point is far from obvious and only few papers deal with this interesting problem. It could be found in [23] that the metal resistivity increase with the temperature has an outstanding influence on the temperature profile around 700°C, while [24] points out no significant effect but around 250°C in the field of domestic appliances. According to [23] and [24], the obtained simulation results showed that radiation and heat conduction could be neglected below 400°C and that the heating time under the inductors is much shorter than the thermal time constant.
Consequently, only convection will be taken into account. Moreover, a kind of compensation between different phenomena can be put in evidence. The material resistivity rises up with temperature and modifies the power density in (5), but the image functions also vary with temperature. As it can be seen in Fig. 10, their modules decrease. Extracted from Flux2D® software, these results show the temperature influence on the real and imaginary parts of the image function of phase 1.

IV. OPEN-LOOP EXPERIMENTAL RESULTS

In Fig. 13 experimental and simulated temperatures are presented in an open-loop condition with ten measurement points along the radius of the disc. These profiles depend on the coil characteristics (impedance, positions) and on the supply currents that feed them.

After two minutes heating, the two profiles are quite similar and the difference between them does not exceed 10%, except close to the centre of the piece where it is very difficult to control the heating process and the temperature. At this point, simulating model has to be slightly improved and in order to be compared again with new experimental results.

V. CURRENT CONTROL

A. PI control

As far as we know, very few works deal with the control of this kind of coupled system [15-19]. A first simplified control scheme is proposed. Fig. 14 describes for one phase, the current control loop for the RMS values of the inductor currents using PI controllers. The RMS current values are calculated by using a passive component circuit composed by a full-wave rectifier and a low-pass filter which bandwidth is set to 100Hz, a kind of trade-off between the bandwidth of the low-pass filter and the bandwidth of the RMS closed loop control.

The PI controllers are tuned according to a pole placement method from three second order small signal models (9)-(11), which derive from open loop experiments and with the help of a parameter off-line identification method based on the least mean square method.

\[
\frac{I_{1,\text{rms}}}{\cos(a_1)} = 103.8 \ e^{-3T_e} + 1.234 E^{-3} s^2
\]

\[
\frac{I_{2,\text{rms}}}{\cos(a_2)} = 131.7 \ e^{-3T_e} + 1.292 E^{-3} s^2
\]

\[
\frac{I_{3,\text{rms}}}{\cos(a_3)} = 128.7 \ e^{-3T_e} + 1.521 E^{-3} s^2
\]

The closed-loop bandwidth is set to 100Hz (<1500 Hz) i.e. lower than the open-loop bandwidth and lower than the switching frequency. It is also set lower than the open-loop bandwidth (=300Hz) because the temperature time constant is very large compared with the current dynamics. The reference RMS values are predetermined for a homogeneous temperature profile and they are reached in few periods i.e. few milliseconds after a 20% step input on their references at 40ms, with low overshoot and no steady-state error. It is important to notice that the power electronic stage does not work according to PWM principles. Given that, inverter currents vary only four times per period, the sample frequency is set to 6 kHz, i.e. four times the system frequency [17]. In simulations, an additional unit delay is included in the closed-loop so as to insert a sampling period delay due to the A/D and D/A conversion times and to the calculation time of the firing angles of the switches inside the FPGA. The \(\cos^1\) term in Fig. 14 allows linearization of the whole loop since the RMS current on inverter \(n^\circ\) is given by (12).

\[
I_{\text{rms}} = \frac{4I_e \cos (a)}{n \sqrt{2}}
\]
The inverter currents ($I_{\text{inv}}$) keep their square waveforms whereas the outputs of PI-controllers ($\alpha_i$) are sampled at 6 kHz (Fig. 16).

Fig. 16. Alpha angles and inverter currents during one period in steady state

To be as close as possible to the experimental conditions, a quantization block is added in the simulation model, the quantization part of the 8bit A/D and D/A components.

Fig. 17. Duty cycles (up) and RMS-values (down) of inductor currents in closed loop with quantization

After some transients on the RMS currents in Fig. 17, the inductor currents in Fig. 18 look like the desired waveforms, i.e. sinusoidal curves with the required amplitudes and phases.

Fig. 18. Three phase inductor currents in closed loop with quantization

The three PI controllers are implemented in a FPGA based control system described in Fig. 19 while the corresponding first closed-loop experimental results could be found in Fig. 20. It is important to notice that the PI controllers are implemented in an old FPGA (FLEX10K20 TC144-4 from Altera®) with a very limited number of elements; as a result, some precision problems occur as it can be seen in Fig. 20 with the small oscillations around the steady state. Nevertheless, the 3 phase RMS currents are controlled around their set points, even in case of sudden dc source current changes (blue curve).
B. RST control

In order to improve the control performance, a RST controller has been designed for each of the 3 phases. Fig. 21 depicts the architecture for one phase, where $I_{13}$ and $I_{1}$ are the coupling terms extracted from (1), and describing the effects of current 2 on phase 1 and of current 3 on phase 1 respectively. The corresponding simulation results are presented in Fig. 22. Thanks to the RST properties and to suitable pole placement without any zero in the closed loop transfer function, the transients show no overshoot and the same time response are observed on the 3 phases and then performance in simulation is improved compared to that of the PI controllers.

This paper presents a simplified but complete and powerful model of the electrical and thermal behaviour of an induction heating multi-phase system taking into account the coupling effects between the phases and the workpiece. The first open loop experimental results on the temperature profile are in rather good agreement with the simulation results and can be seen as a first step for model validation. The flexibility of this system is an important asset, so digital control makes it possible. The first current controllers give rather good closed loop performance in continuous and digital conditions. Future works will tackle the closed-loop control of temperature in the material to be heated, the soft-switching mode for the power electronic stage, the studies are currently in progress. Moreover, the current control itself could be improved with a state space decoupling method which aims at making the inductor currents completely independent of each other whatever the reference point.

REFERENCES


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