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Industrial water management by multiobjective optimization: from individual to collective solution through eco-industrial parks

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Abstract

Industrial water networks are designed in the first part by a multiobjective optimization strategy, where fresh water, regenerated water flow rates as well as the number of network connections (integer variables) are minimized. The problem is formulated as a Mixed-Integer Linear Programming problem (MILP) and solved by the ε-constraint method. The linearization of the problem is based on the necessary conditions of optimality defined by Savelski and Bagajewicz (2000). The approach is validated on a published example involving only one contaminant. In the second part the MILP strategy is implemented for designing an Eco-Industrial Park (EIP) involving three companies. Three scenarios are considered: EIP without regeneration unit, EIP where each company owns its regeneration unit and EIP where the three companies share regeneration unit(s). Three possible regeneration units can be chosen, and the MILP is solved under two kinds of conditions: limited or unlimited number of connections, same or different gains for each company. All these cases are compared according to the global equivalent cost expressed in fresh water and taking also into account the network complexity through the number of connections. The best EIP solution for the three companies can be determined.

1. Introduction

During the last decades, many developed countries have increased their investment in environmental research and development due to an increasing depletion of natural resources such as fresh water for instance (UNESCO, 2009). With the increasing interest for global environment preservation, the unlimited resources paradigm became little by little obsolete. In 2008, the global needs in fresh water were estimated to be 4000 km³ (UNESCO, 2009), where 20% were used by industry and have been globally increased by a factor of four during the last 50 years (Oecd, 2008). The environmental impact induced by the process industry is linked both to the high volumes involved and to the diversity of toxic products generated along the processing chain. Consequently, a real need to define optimized water networks so as to reduce the impact of contaminants on the environment, has recently emerged.

Although the world concern of sustainable development gave birth to a lot of works during the last decades, the concept of Industry linked to Ecology is quite much older. Indeed, since the beginning of the twentieth century, scientists are worried about designing clean industries. Several studies stated the recycling of by-products of an industry by another one (Simmonds, 1862; Conover, 1918). These studies did not introduce any of financial term on what they dealt for. “Industrial Ecology” really appeared (Hoffman, 1971) in the 1970’s and Japanese and Belgian studies went deeper in this topic (Watanabe, 1972; Gussow and Meyers, 1970). However, Frosch and Gallapoulos (1989) popularized this term twenty years ago from the idea that we should use the analogy of natural systems as an aid in understanding how to design sustainable industrial systems. As they indicate the ideal ecosystem, in which the use of energy and materials is optimized, wastes and pollution are minimized and there is an economically viable role for every product of a manufacturing process, will not be attained soon. It was true in 1989, and it is always true today.

Industrial Ecology has been defined by Allenby (2006) as “a systems-based, multidisciplinary discourse that seeks to understand emergent behaviour of complex integrated human/natural systems”. In most of the researches in Industrial Ecology the common guideline is that natural systems do not have waste in
them, so our systems should be modeled from natural ones if we want them to be sustainable.

Without falling into the trap of abstruse ecological discourses, many difficult societal and/or industrial problems appear under the generic term of Industrial Ecology. Building a sustainable industry is slightly linked to the term Industrial Symbiosis. According to Chertow (2000), an industrial symbiosis engages “separate industries in a collective approach to competitive advantage involving physical exchange of materials, energy, water and by-products”. A primordial feature of an industrial symbiosis is the collaboration offered by the geographic proximity of the several companies. Most widespread manifestations of an industrial symbiosis are Eco-Industrial Parks. The term “eco-industrial park” is the subject of many debates due to its definition, difficult to formulate rigorously. However, a definition commonly adopted is “an industrial system of planned materials and energy exchanges that seeks to minimize energy and raw materials use, minimize waste, and build sustainable economic, ecological and social relationships” (PCSD, 1996; Alexander et al., 2000). This definition was later reported by Côté and Cohen-Rosenthal (1998). Obviously, a basic condition for an EIP to be economically viable is to demonstrate that the sum of benefits achieved by working as collective is higher than working as a stand-alone facility.

There is some amount of uncertainty in this type of optimization model. For instance, the mass loads of contaminants for water-reusing processes or any other parameter that may change during the operation process. Although some studies (Sahinidis, 2004; Karuppiah and Grossmann, 2008) have incorporated these uncertainties to design industrial water networks, the objectives of this study.

The first part of this paper aims at defining a general methodology by taking into account only the single contaminant case for the Design of Water Networks (DWN). The generic problem is formulated under a MILP form with integer variables related to the connections into the network. The biobjective optimization of the fresh water flow rate at the network entrance and the water flow rate at regeneration unit inlets, parameterized by the number of connections, is carried out according to a lexicographic procedure. The approach, validated on a published example involving ten processes and one regeneration unit, is extended in the second part to eco-industrial parks (EIP). The last part deals with several EIP configurations in order to evaluate the feasibility of each solution.

2. Previous works

Historically, the design of water network (DWN) was carried out not for EIP purposes, but for a stand-alone company by means of graphical methodologies (Dunn and Wenzel, 2001; Jacob et al., 2002; Linhoff and Vredeveld, 1984; Manan et al., 2006; Wan Alwi, 2008), mathematical programming (Bagajewicz and Savelski, 2001; Feng et al., 2008; Huang et al., 1999) and synthesis of mass exchange networks (El-Halwagi, 1997; Hallale and Fraser, 2000; Shafiei et al., 2004). Designing water networks refers to allocate the streams of the networks between several units while respecting constraints and satisfying objectives. Water allocation problems (WAP) were widely studied during the last decades due to the growing interest for sustainable development in industries (de Faria and de Souza, 2009; Kumaraprasad and Muthukumar, 2009; Klemes et al., 2010; Poplewski et al., 2010). Linear formulations implemented for maximizing water regeneration and reuse into industrial processes has been first developed in a lot of previous works (Bagajewicz and Savelski, 2001; El-Halwagi, 1997; El-Halwagi et al., 2004; Wang and Smith, 1994). These techniques are limited to simple contaminant networks (Gomes et al., 2007), which are the main subject of the present study. Another strategy has already been adopted regarding the resolution of WAP, it consists in multiobjective optimization using genetic algorithm (Lavric et al., 2005). Nonlinear strategies based on the relaxation of the bilinear terms involved in the balance equations are presented in the works of Quesada and Grossmann (1995) and Galan and Grossmann (1998). Even if significant advances have been performed in the field on nonlinear mixed-integer
programming, the search for a solution of a linear problem is always easier than in the nonlinear case. This concerns both the global optimality of the solution found, and the ease to initialize the search. Furthermore, MILP methods may support important numbers of variables and high combinatorial aspects. These issues are important when dealing with EIPs. In most of previous works, DWN was carried out only for monocontaminant networks, but in a recent paper Boix et al. (2011) deal with multicontaminant problems. In that case, the MILP problem becomes a MINLP one; that is the reason why this study is restricted to the monocontaminant case.

EIP problems for managing industrial water were solved by mathematical programming either by using NLP (NonLinear Programming), MILP (Mixed-Integer linear Programming) or MINLP (Mixed-Integer NonLinear programming) procedures (Aviso et al., 2010a, 2010b; Chew et al., 2008, 2010a, 2010b; Lovelady and El-Halwagi, 2009; Kim et al., 2010). What is giving cause for concern in numerous research works is to deal with conflicting objectives (Erol and Thöming, 2005). However, new strategies have been adopted in order to compensate for this problem like a bi-level fuzzy optimization developed by Aviso et al. (2010a, 2010b). Furthermore, a lot of research has been devoted to develop some indicators to evaluate the satisfaction of each participant of the IEP (Tiejun, 2010; Zhu et al., 2010). Other recent works implement the game theory for solving the problem (Chew et al., 2009, 2010c) and various approaches consider that an EIP is comparable to biological or ecological natural systems (Liwarska-Bizukojc et al., 2009; Tiejun, 2010). All these studies choose classical objectives: the fresh water consumption or the satisfaction of participants but Lim and Park (2008) focused on the necessity of reducing the total carbon footprint of participant’s water supply systems.

However EIPs have to face two main classes of challenges that can determine their development. The former is the Technical/Economic challenge: if the exchanges among the participants are unfeasible, no EIP can be successful. Indeed a real connectivity must exist between the companies within the EIP. The latter related to the organizational/commercial points can represent the biggest hurdle. However this second thorny issue will not be tackled in this paper related to the implementation of an EIP for managing industrial waters. Chertow identified that certain precursors of symbiosis can be regeneration or waste water reuse and can lead to more extensive symbiotic cooperation as well (Chertow, 2007).

Several successful examples of EIPs located all around the world particularly in North America (Côté and Cohen-Rosenthal, 1998; Gibbs and Deutz, 2005, 2007; Heeres et al., 2004), Western Europe (Baas and Boons, 2004; Heeres et al., 2004; Mirata, 2004; Van Leeuwen et al., 2003), and Australia (Roberts, 2004; Van Beers et al., 2007; Van Berkel, 2007; Giurco et al., 2010). More recently, new eco-parks have been implanted in other countries such as China (Geng and Hengxin, 2009; Liu et al., 2010; Shi et al., 2010),

Fig. 1. Superstructures for a company (a), and an EIP (b).
3. Multiobjective MILP problem

3.1. Problem statement

Given a set of regeneration units and processes, the objective is to determine a network of connections of water streams among them so that both the overall fresh water consumption and the regenerated water flow rate are minimized. Each process has limited inlet and outlet concentrations and regeneration units are defined by their outlet concentration. The particular case of an EIP can be assimilated to a bigger company divided into blocks (each block is in fact a company). The purpose is to design an optimal network (for a company or for an EIP) where all the requirements in terms of contaminant concentrations for each process are respected.

3.2. Superstructures definition

In the company superstructure, all the possible connections between processes and regeneration units may exist, except recycling to the same regeneration unit or process. For each water-using process, input water may be fresh water, used water coming from other processes and/or recycled water; the output water for such a process may be sent towards the discharge, or to other processes and/or to regeneration units. Similarly, for a regeneration unit, input water may come from processes or from other regeneration units. Regenerated water may be reused in the processes or sent towards other regeneration units. (Fig. 1a) In order to define a generic formulation, the physical or chemical operation (reaction, separation...) performed in each process is not taken into account. However, a process j generates a mass of contaminant due to its own working. This contamination is expressed in g/h and noted: \( M_{j\rightarrow i} \), this value imposed by the process itself, is fixed by the user.

The same superstructure is also adopted for each company involved in an EIP (Fig. 1b) and the connections between the different companies will be defined in Section 4 where several examples are studied.

3.3. Process modelling

In most previous works, the water allocation problem is generally solved with an MINLP optimization (Feng et al., 2008). Indeed, the model-based problem contains bilinear terms due to products in mass balances for contaminants. These bilinearities are caused by the products of concentrations and flow rates (Sienutycz and Jezowski, 2009).

In this study, the formulation is based upon the necessary conditions of optimality developed by Savelski and Bagajewicz (2000) that relies on the elimination of these bilinearities for a single contaminant water network. The modeling equations are the same as used in Boix et al. (2010), involving partial mass flows; that is to say that contaminants are represented by flow rates (in g/h) instead of concentrations (in ppm). The partial contaminant flow rate is linked to the contaminant concentration also involving the partial water flow rate (in T/h) by this definition (assuming a flow stream going from process \( p \) to process \( k \)):

\[
\frac{w_{i}^{p\rightarrow k}}{w_{i}^{p\rightarrow k} + w_{i}^{\rightarrow k}} = C_{i}^{p\rightarrow k}
\]

(1)

The denominator: \( w_{i}^{p\rightarrow k} + w_{i}^{\rightarrow k} \) represents the total flow rate of the stream. This term can be reduced regarding units of flow rates. Indeed, \( w_{i}^{p\rightarrow k} \) is expressed in T/h whereas \( w_{i}^{\rightarrow k} \) unit is g/h \((10^{-6} \text{ T h}^{-1})\) what supports the relation (2) and leads to the Equation (3) giving the definition used in this study for a partial contaminant flow rate.

\[
\frac{w_{i}^{p\rightarrow k}}{w_{i}^{p\rightarrow k} + w_{i}^{\rightarrow k}} = C_{i}^{p\rightarrow k} \times w_{i}^{\rightarrow k}
\]

(2)

As a result of these assumptions, the mass balances for flow rates are written as follows:

- For a given process \( j \), the inlet water (\( i = 1 \)) flow rate is equal to the outlet water flow rate:

\[
\begin{align*}
  w_{i}^{j} + \sum_{k} w_{i}^{p\rightarrow j} + \sum_{m} w_{m}^{j\rightarrow m} & = w_{i}^{j} + \sum_{k} wp_{i}^{p\rightarrow j} \\
  & + \sum_{m} wp_{i}^{j\rightarrow m}
\end{align*}
\]

(3)

- For a given process \( j \), the inlet contaminant (\( i > 1 \)) flow rate plus the contaminant mass load is equal to the outlet contaminant flow rate:

\[
\begin{align*}
  w_{i}^{j} + \sum_{k} wp_{i}^{p\rightarrow j} + \sum_{m} wp_{i}^{j\rightarrow m} & = w_{i}^{j} + \sum_{k} wp_{i}^{p\rightarrow j} \\
  & + \sum_{m} wp_{i}^{j\rightarrow m}
\end{align*}
\]

(4)

- For a given regeneration unit \( m \), the inlet water flow rate is equal to the outlet water flow rate:

\[
\begin{align*}
  w_{i}^{m} + \sum_{j} wp_{i}^{j\rightarrow m} & = w_{i}^{m} + \sum_{j} wp_{i}^{j\rightarrow m} \\
  & + \sum_{n} wp_{i}^{j\rightarrow n}
\end{align*}
\]

(5)

- For a given regeneration unit \( m \), the inlet contaminant flow rate is equal to the outlet contaminant flow rate:

\[
\begin{align*}
  w_{i}^{m} + \sum_{j} wp_{i}^{j\rightarrow m} & = w_{i}^{m} + \sum_{j} wp_{i}^{j\rightarrow m} \\
  & + \sum_{n} wp_{i}^{j\rightarrow n}
\end{align*}
\]

(6)

- The overall fresh water flow rate is equal to the total discharged water flow rate:

\[
\sum_{m} \text{wr}_{i}^{m} + \sum_{j} \text{wr}_{i}^{j} = \sum_{j} \text{wr}_{i}^{j}
\]

(7)

Brazil (Veiga et al., 2009) or Korea (Oh et al., 2005; Park et al., 2008). A good review of several successful of EIP had been raised by Tudor et al. (2007).

As cited by Tibbs (1993) about the creation of industrial ecosystems “Industrial ecosystems are a logical extension of life-cycle thinking, moving from assessment to implementation. They involve “closing loops” by recycling, making maximum use of recycled materials in new production, optimizing use of materials and embedded energy, minimizing waste generation, and reevaluating “wastes” as raw material for other processes.” The present work, related to the management of industrial water, comes within this scope. Furthermore from Baas (2006) and Sakre et al. (2011), this study is situated at the micro level of the Cleaner Production Systems.
- The total discharged contaminant flow rate is equal to the sum of contaminant mass loads of each process j:

$$\sum_m w_{pd,j} = \sum_i w_{d,j,i} = \sum_i M \delta_i$$  \hspace{1cm} (9)

Equations (10) and (11) introduce two new notations for the total inlet and outlet flow rates in a given process j in order to make the understanding of the next constraints easier:

$$w_j + \sum_k w_{j,k} = w_{p, jak}$$ \hspace{1cm} (10)

$$\sum_k w_{j,k} + \sum_m w_{p,j,m} + w_{d,j} = w_{p, j, out}$$ \hspace{1cm} (11)

Given this set of mass balances equations, constraints on contaminant concentrations are added to the mathematical problem. Each process is limited within inlet and outlet contaminant concentrations following these inequalities (for a process j):

$$w_{p, jak} \leq C_{max,k} \times w_{d,j}$$ \hspace{1cm} (12)

$$w_{p, j, out} \leq C_{max,j} \times w_{p, j, out}$$ \hspace{1cm} (13)

In the same way, the post-regeneration concentration is fixed and gives birth to the equality (14).

$$w_{p, out,j} = C_{r, out} \times w_{p, out,j}$$ \hspace{1cm} (14)

The addition of the constraint (13) is not without repercussions because it represents mass balances at splitters. Consequently, the output streams of a given process must have the same pollutant concentration and this assumption is mathematically conveyed for the outlet of a process j as:

$$w_{p, j, out} - C_{max,j} \times w_{p, j, out} = w_{p, j, m} - C_{max,j} \times w_{p, j, m}$$ \hspace{1cm} (15)

And in the same way, for the regeneration unit m:

$$w_{p, j, in} - C_{r, m} \times w_{p, j, in} = w_{p, j, m} - C_{r, m} \times w_{p, j, m}$$ \hspace{1cm} (16)

However, these equalities hide an important condition. Indeed, if the mass flow of water is null for one stream, this stream does not exist, what is traduced by the logic condition (17):

$$w_{p, j, k} = 0 \implies w_{p, j, k} = 0 \hspace{1cm} (17)$$

It changes Equation (15) in Equation (18), if the process j does not distribute water to another process k, it implies that, for instance:

$$0 = w_{p, j, m} - C_{max,j} \times w_{p, j, m} = w_{d,j} - C_{max,j} \times w_{p, j, out}$$ \hspace{1cm} (18)

Thus,

$$w_{p, j, in} = C_{max,j} \times w_{p, j, m}$$ \hspace{1cm} (19)

The former demonstration changes Equation (19) into the equality (19), and thus, implies that outlet concentrations are equal to the maximal value $C_{max,p}$ for each process of the network. This condition does not compromise the guarantee of optimality because written like this, the problem check all the “necessary optimality conditions” for a single contaminant water allocation problem (Savelski and Bagajewicz, 2000). These authors give several theorems among which:

- “Theorem 2: If a solution of the WAP problem is optimal, then the outlet concentration of a head process is equal to its maximum or an equivalent solution with the same overall fresh water exists in which the concentration is at its maximum.”

- “Theorem 3: If a solution of the WAP problem is optimal, then the outlet concentration of an intermediate process reaches its maximum or an equivalent solution with the same overall fresh water exists in which the concentration is at its maximum.”

- “Theorem 4: If the solution of the WAP problem is optimal, then the outlet concentration of a terminal process is equal to its maximum or an equivalent solution with the same overall fresh water consumption exists.”

In a water network, since all processes are either head, intermediate or terminal processes, the constraint (18) agrees with the necessary optimality conditions proved by Savelski and Bagajewicz (2000). At this stage of the modelling process, the problem is linear and can be solved with a Linear Programming (LP).

Nevertheless, in order to evaluate the network complexity, a binary variable is allocated to each flow, what changes the problem into a MILP form. These variables are added in the program with the help of a Big-U constraint as (U has to be bigger than any water flow rate of the plant):
one. Consequently, it is better to let $F_1$ and $F_2$ as two separate objectives in order to construct Pareto fronts. Indeed, a cost value can change in function of the capacities or yet the geographic situation of the company. In this multiobjective optimization framework all the treated results are presented first and a tool for decision aid is then proposed and used. The advantage of this method is to have universal results that can be treated with several tools. Furthermore, $F_3$ is deliberately estimated in terms of connections number because if a cost is attributed, the objective function cannot stay linear. According to Sieniutycz and Jezowski (2009), the cost of connections is linked to the associated flow rate according a power law (23). Thereby, the problem is changed into a nonlinear form. It is worth noting that the results can be evaluated in terms of cost in a post-optimization stage.

$$C = \gamma \times \left(W_i^f\right)^\mu$$

(23)

Where $C$ is the cost of a connection linked to the flow rate $W_i^f$; $\mu$ and $\gamma$ are coefficients depending on the parameters of the network studied (flow rates, type of liquid circulating...).

The optimization variables are the various flow rates (continuous variables) and the existence of connections (binary variables). The additional set of constraints is given by the modelling equations. The problem solutions are displayed in the form of a Pareto front, so a comparison strategy has to be defined for identifying "good" solutions among the ones reported on the front.

### 3.5. Comparison strategy

In what follows, internal connections refer to connections between processes of the same company and external connections are related to connections coming from or going towards other companies. By supposing constant distances between companies, it is assumed that for each external connection, the cost for each company is divided by two. For EIPs involving an interceptor for sharing regeneration units, the connections between a given company and the interceptor are external connections. Thus, the equivalent number of connections ENC for a given company, which reflects the piping and pumping costs and the associated infrastructure, is given by:

$$ENC = \text{number of internal connections} + 0.5 \times \text{number of external connections}$$

(24)

Another economic indicator, the Global Equivalent Cost (GEC) in water flow rate, is defined in this study. This cost is expressed as an equivalent of water flow rate in T/h. For comparison purposes, we could use the prices of fresh water, of regenerated water and of post-treatment in the waste. However, these prices are strongly linked to the country and even to regions of this state.

$$\text{GEC} = F_1 + R + W$$

(25)

where $F_1$ is defined above, $R$ and $W$ are the contributions of regenerated and waste waters, with:

$$R = \alpha \times F_2 \quad \text{and} \quad W = \beta \times F_W$$

(26)

where $F_W$ is the waste water flow rate.

Combining relations (25) and (26) leads to the following relation:

$$\text{GEC} = F_1 + \alpha \times F_2 + \beta \times F_W$$

(27)

In the previous relations, $\alpha$ depends on the type of regeneration unit (see Table 1) and $\beta = 5.625$ according to Bagajewicz and Faria (2009).

### 3.6. Economic impact of connections

The economic impact of the number of connections on the choice of a particular solution is analyzed from the following example: a company involving five processes, with a regeneration unit of type I and eight connections. The same flow ($23.25$ T h$^{-1}$) is assumed in each pipe, and the piping cost is computed from Chew et al. (2008) with a mean length of internal pipes of $50$ m, a fractional interest rate of $5\%$, a period of $5$ years and a fresh water cost of $0.1 \text{€}/\text{T}$ (cost of river water). The ratio (piping cost/water cost) is $14\%$. Even if the network exhibits simplicity of implementation, this example shows that there is a real economic interest in optimizing the number of connections. Note that when EIPs are considered, the part due to external connections which are much longer (there is at least a factor $10$) than the internal ones, significantly increases the ratio (piping cost/water cost).

### 4. Design of water network problem

#### 4.1. Problem formulation

For the example presented below, the number of connections in the network is defined in the range $[11-120]$ representing the lowest (respectively the highest) number of possible connections in the network. This water allocation problem consists in solving the biobjective problem $(F_1, F_2)$ under the constraint $F_3$ fixed to a given value in the previous range. The biobjective method recalled in Section 3.4 and based on the $\epsilon$-constraint two-phase strategy (Mavrotas, 2009) is implemented. During the first phase, the first objective ($F_1$) is minimized alone, while the second one ($F_2$) is introduced as a bounding constraint. The second objective is minimized in the second step, where the first one can vary in an interval for which the optimal value obtained in the first phase is the median. When the solutions obtained in the two phases are identical, they are inserted in the Pareto front.

This example involving ten processes, one regeneration unit of type I (see Table 1) and one contaminant, was already proposed by Bagajewicz and Savelski (2001), the corresponding limiting process data are shown in Table 2 and the outlet regeneration concentration is fixed at $5$ ppm. The corresponding MILP involves $143$ binary variables related to connections, $332$ continuous variables and $351$ constraints.

#### 4.2. Theoretical results

The biobjective optimization was performed for different values of the connection number $F_3$ in the range $[11,120]$. The constraint (18) imposes to minimize the overall fresh water consumption. Hence, for several ranges of $F_2$, the fresh water consumption is minimized in order to have one optimal solution for each range of $F_2$ and for a given value of $F_3$. Starting from $F_3 = 11$, all the possible values for $F_2$ were tested. When $F_3$ is greater or equal to 19, all the

<table>
<thead>
<tr>
<th>Table 1 Values of $\alpha$ according to types of regeneration units.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Regeneration type</td>
</tr>
<tr>
<td>I</td>
</tr>
<tr>
<td>II</td>
</tr>
<tr>
<td>III</td>
</tr>
</tbody>
</table>

After the multiobjective optimization step, the different solutions are discriminated by performing a Pareto sort on the couples (GEC, ENC) for each company.
fronts are superimposed on the same straight line. For example, the Pareto fronts corresponding to $F_3 = 11, 12, 19$ and 120 are reported in Fig. 2. Feng et al. (2007) show the linearity of the Pareto fronts for this particular problem. The values obtained for this example are identical with the ones reported in the literature (Bagajewicz and Savelski, 2001; Feng et al., 2008; Huang et al., 1999). Thus the network mathematical formulation and the optimization procedure are validated.

4.3. Choice of the best feasible network

The solutions displayed in Fig. 2 are only theoretical results because in some cases, connections with quasi-null flow rates may exist. Obviously this type of solution cannot be considered in practice. Indeed, it is generally admitted (Bagajewicz and Savelski, 2001) that networks involving flows lower than 2 T h$^{-1}$ cannot be used in practice because they force the user using very small pipes (with a diameter of about 1 inch). These pipes are not economically profitable regarding their investment cost. From the theoretical study, “good” solutions on an industrial point of view, combining moderate GEC, few connections and non null flow rates in the connections have to be defined. The minimum value of GEC was studied vs. the connection numbers, and the best solution (GEC = 619 T h$^{-1}$) is obtained with 17 connections and corresponds to: $F_1 = F_{w1} = 10$ T h$^{-1}$ and $F_2 = 177$ T h$^{-1}$. The flowsheet of the proposed solution is given in Fig. 3 (connections are numbered in brackets; connections going to the waster are not numbered). Other solutions with higher connection numbers can be also identified, but are topologically more complicated.

4.4. Discussion

From this example, the following conclusions can be emphasized: (i) the solutions provided by the Pareto fronts are only theoretical results; ii) further investigations based on the global equivalent cost (GEC) and the connection number have to be performed for identifying the best practical solution; iii) since it does not requires any initialization phase and can tackle large scale problems, this MILP approach can be implemented to optimize EIPs, where the problems are larger in terms of numbers of variables and constraints.

5. EIPs for managing industrial waters

5.1. Problem formulation

The DWN procedure is now extended to the design of EIPs and illustrated by the example proposed by Olesen and Polley (1996). The industrial pool involves three companies, each one including five processes; the data are displayed in Table 3. The three companies decide to constitute an EIP for managing their used waters. Three scenarios are considered: EIP without regeneration unit, EIP where each company owns its regeneration unit and EIP where the three companies share regeneration unit(s). Three possible regeneration units (see Table 1) can be chosen under two kinds of constraints: limited or unlimited number of

<table>
<thead>
<tr>
<th>Process</th>
<th>$C_{\text{max}}^\text{in}$ (ppm)</th>
<th>$C_{\text{max}}^\text{out}$ (ppm)</th>
<th>$M_j^i$ (g/h)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>25</td>
<td>80</td>
<td>2000</td>
</tr>
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<td>200</td>
<td>4000</td>
</tr>
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<td>4</td>
<td>50</td>
<td>100</td>
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</tr>
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<td>5</td>
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<td>800</td>
<td>30000</td>
</tr>
<tr>
<td>6</td>
<td>400</td>
<td>800</td>
<td>5000</td>
</tr>
<tr>
<td>7</td>
<td>400</td>
<td>600</td>
<td>2000</td>
</tr>
<tr>
<td>8</td>
<td>0</td>
<td>100</td>
<td>1000</td>
</tr>
<tr>
<td>9</td>
<td>50</td>
<td>300</td>
<td>20000</td>
</tr>
<tr>
<td>10</td>
<td>150</td>
<td>300</td>
<td>6500</td>
</tr>
</tbody>
</table>
connections, same or different gains for each company. The objective is then to identify the best strategy for each company so as to minimize the global equivalent cost in fresh water and the number of connections in the network. Compared to some basic cases, a solution will be retained only if the gain in GEC for each company is positive, and for two equivalent gains, the solution with a minimum ENC will be selected. Table 4 explains the several cases which are explored all along the Section 5. The results are displayed in Table 5, where only the cases giving a positive gain in GEC compared to the basic case for the three companies are reported. The rejected solutions are reported in Table 6 and will not be discussed in the following sub-sections.

5.2. Basic case: companies without EIP and without regeneration unit (case 1)

This preliminary study (case 1) concerns the individual optimization of the water network for each company without considering the EIP, according to objectives $F_1$ and $F_3$ (since there is no regeneration unit, the objective $F_2$ is not taken into account). The results of this monobjective optimization problem are displayed in Table 5, and for the sake of illustration, the network flowsheet for company A with six connections is displayed in Fig. 4.

5.3. EIP without regeneration unit (cases 2–4)

The three companies which have no regeneration unit constitute an EIP without regeneration unit, but by allowing their used waters to be treated in the two other companies and receiving used

![Fig. 3. Best solution for the water allocation problem (flows are in T/h).](image)

### Table 3

Process characteristics for the EIP.

<table>
<thead>
<tr>
<th>Process</th>
<th>Company</th>
<th>Contaminant flow rate (Kg/h)</th>
<th>Maximal inlet concentration (ppm)</th>
<th>Maximal outlet concentration (ppm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>A</td>
<td>2</td>
<td>0</td>
<td>100</td>
</tr>
<tr>
<td>2</td>
<td>2</td>
<td>50</td>
<td>80</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>3</td>
<td>50</td>
<td>100</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>4</td>
<td>30 80</td>
<td>800</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>5</td>
<td>400</td>
<td>800</td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>B</td>
<td>2</td>
<td>0</td>
<td>100</td>
</tr>
<tr>
<td>7</td>
<td>2</td>
<td>50</td>
<td>80</td>
<td></td>
</tr>
<tr>
<td>8</td>
<td>5</td>
<td>80</td>
<td>400</td>
<td></td>
</tr>
<tr>
<td>9</td>
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<td>800</td>
<td></td>
</tr>
<tr>
<td>10</td>
<td>4</td>
<td>400</td>
<td>1000</td>
<td></td>
</tr>
<tr>
<td>11</td>
<td>C</td>
<td>2</td>
<td>0</td>
<td>100</td>
</tr>
<tr>
<td>12</td>
<td>2</td>
<td>25</td>
<td>50</td>
<td></td>
</tr>
<tr>
<td>13</td>
<td>5</td>
<td>25</td>
<td>125</td>
<td></td>
</tr>
<tr>
<td>14</td>
<td>30</td>
<td>50</td>
<td>800</td>
<td></td>
</tr>
<tr>
<td>15</td>
<td>15</td>
<td>100</td>
<td>150</td>
<td></td>
</tr>
</tbody>
</table>

### Table 4

Superstructure Characteristics of the cases treated.

<table>
<thead>
<tr>
<th>Superstructure</th>
<th>Cases</th>
<th>Description of the configuration</th>
</tr>
</thead>
<tbody>
<tr>
<td>Without EIP</td>
<td>Case 1</td>
<td>Companies are considered individually and are not included in the EIP</td>
</tr>
<tr>
<td></td>
<td>Case 2</td>
<td>Connections are not included as an objective, $F_1$ is free</td>
</tr>
<tr>
<td>EIP without regeneration unit</td>
<td>Case 3</td>
<td>Connections are restricted to 21, the minimum feasible</td>
</tr>
<tr>
<td></td>
<td>Case 4</td>
<td>Connections are restricted to 21 and each company needs to have the same gain</td>
</tr>
<tr>
<td>EIP with individual regeneration units (direct integration scheme)</td>
<td>Case 5</td>
<td>Companies are considered individually to choose their own regeneration unit</td>
</tr>
<tr>
<td></td>
<td>Case 6</td>
<td>Connections are not included as an objective, $F_3$ is free</td>
</tr>
<tr>
<td></td>
<td>Case 7</td>
<td>Connections are restricted to 26, the minimum feasible</td>
</tr>
<tr>
<td></td>
<td>Case 8</td>
<td>Connections are restricted to 26 and each company needs to have the same gain</td>
</tr>
<tr>
<td>EIP with a shared regeneration unit (indirect integration scheme)</td>
<td>Case 9</td>
<td>EIP with regeneration unit of type I</td>
</tr>
<tr>
<td></td>
<td>Case 10</td>
<td>EIP with regeneration unit of type I and external connections are restricted to 2</td>
</tr>
<tr>
<td></td>
<td>Case 11</td>
<td>EIP with an interceptor containing regenerations of type I, II and III</td>
</tr>
<tr>
<td></td>
<td>Case 12</td>
<td>Case 11 with connections restricted to 26 and the same gain for each company</td>
</tr>
<tr>
<td></td>
<td>Case 13</td>
<td>Case 11 with connections restricted to 31 and the same gain for each company</td>
</tr>
</tbody>
</table>

Summarization of the several cases treated in Section 6.
waters from the two other companies, as shown in Fig. 5 (do not take into account the dotted lines, nor italic parts). Three cases are considered: case 2 corresponds to an unlimited number of connections in the EIP; in case 3 the number of connections is assumed to be restricted to 21, which is the best solution found in case 1 (6 for company A, 8 for company B and 7 for company C, see Table 4); in case 4 the number of connections is also limited to 21 and the same relative gain is assumed for each company.

The results are displayed in Table 5, where the gains are computed by using case 1 as a basis. Only the case 4 (same relative gain in GEC for each company, and also the same number of connections, 21), gives a positive gain (4.3%) for each company. The new flowsheet for company A in the case 4 is depicted in Fig. 6, where external connections are numbered in brackets, italic.

5.4. EIP with one regeneration unit per company (direct integration, cases 5–8)

Each company is now equipped with its own regeneration unit chosen among the three types above mentioned. In the basic case 5, the DWN problem is solved for each company without considering the EIP in order to determine the best regeneration unit chosen among the three types listed in Table 1. From this multiobjective optimization study (objectives $F_1$, $F_2$ and $F_3$), the best solution is obtained when companies A and B choose regeneration unit I, and company C, regeneration unit II. These solutions are given by the median points of the Pareto fronts ($F_1$, $F_2$) for the minimal values of $F_3$, and the results are displayed in Table 5.

Then the three companies constitute an EIP without common regeneration unit, but by allowing their polluted streams to be treated either in their own regeneration unit, or in the two other companies (see Fig. 5, do not take into account the dotted lines). Three new cases are considered: case 6 with no limitation on the number of connections, case 7 with the same number of connections less equal than the best solution of case 5 (26, i.e. 8 for

<table>
<thead>
<tr>
<th>Case</th>
<th>$F_1$ T/h</th>
<th>$F_w$ T/h</th>
<th>$F_3$ T/h</th>
<th>GEC T/h</th>
<th>Gain % Case 1</th>
<th>Gain % Case 5</th>
<th>Int. + Ext. conn</th>
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</thead>
<tbody>
<tr>
<td>A case 1</td>
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<td>98.3</td>
<td>xxx</td>
<td>651</td>
<td>xxx</td>
<td>xxx</td>
<td>6</td>
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<tr>
<td>A case 4</td>
<td>102.8</td>
<td>92.6</td>
<td>xxx</td>
<td>623</td>
<td>4.3</td>
<td>xxx</td>
<td>6</td>
</tr>
<tr>
<td>A case 5</td>
<td>20</td>
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<td>166</td>
<td>195</td>
<td>70.0</td>
<td>xxx</td>
<td>8</td>
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<tr>
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<td>15.2</td>
<td>166.6</td>
<td>168</td>
<td>74.2</td>
<td>13.8</td>
<td>7</td>
</tr>
<tr>
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<td>20</td>
<td>19</td>
<td>188</td>
<td>362</td>
<td>71.1</td>
<td>3.6</td>
<td>9</td>
</tr>
<tr>
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<td>54.6</td>
<td>54.6</td>
<td>xxx</td>
<td>346</td>
<td>4.3</td>
<td>xxx</td>
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<td>45</td>
<td>53.6</td>
<td>xxx</td>
<td>157</td>
<td>56.6</td>
<td>8</td>
<td></td>
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<tr>
<td>B case 5</td>
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<td>128</td>
<td>135</td>
<td>62.4</td>
<td>13.8</td>
<td>9</td>
</tr>
<tr>
<td>B case 8</td>
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<td>67</td>
<td>151</td>
<td>76.8</td>
<td>12</td>
<td></td>
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<tr>
<td>C case 1</td>
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<td>190</td>
<td>xxx</td>
<td>1259</td>
<td>xxx</td>
<td>7</td>
<td></td>
</tr>
<tr>
<td>C case 4</td>
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<td>182</td>
<td>xxx</td>
<td>1204</td>
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<td>404</td>
<td>67.9</td>
<td>13.8</td>
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</tr>
<tr>
<td>C case 13</td>
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<td>213</td>
<td>452</td>
<td>30.6</td>
<td>3.6</td>
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<tr>
<td>Total case 1</td>
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<td>343</td>
<td>xxx</td>
<td>2272</td>
<td>xxx</td>
<td>21</td>
<td></td>
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<tr>
<td>Total case 4</td>
<td>328</td>
<td>328</td>
<td>xxx</td>
<td>2173</td>
<td>4.3</td>
<td>xxx</td>
<td>21</td>
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<tr>
<td>Total case 5</td>
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<td>60</td>
<td>426</td>
<td>821</td>
<td>63.9</td>
<td>xxx</td>
<td>26</td>
</tr>
<tr>
<td>Total case 8</td>
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<td>60</td>
<td>409</td>
<td>708</td>
<td>68.8</td>
<td>13.8</td>
<td>26</td>
</tr>
<tr>
<td>Total case 13</td>
<td>60</td>
<td>60</td>
<td>446</td>
<td>791</td>
<td>65.2</td>
<td>3.6</td>
<td>31</td>
</tr>
</tbody>
</table>

Table 6

<table>
<thead>
<tr>
<th>Rejected solution</th>
<th>Gain % vs. Case 1</th>
<th>Gain % vs. Case 5</th>
</tr>
</thead>
<tbody>
<tr>
<td>C case 2</td>
<td>−8.2</td>
<td>xxx</td>
</tr>
<tr>
<td>B case 3</td>
<td>−10.5</td>
<td>xxx</td>
</tr>
<tr>
<td>C case 3</td>
<td>−2.6</td>
<td>xxx</td>
</tr>
<tr>
<td>A case 6</td>
<td>xxx</td>
<td>−10.2</td>
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<tr>
<td>B case 6</td>
<td>xxx</td>
<td>−61.8</td>
</tr>
<tr>
<td>A case 7</td>
<td>xxx</td>
<td>−74.9</td>
</tr>
<tr>
<td>A case 9</td>
<td>xxx</td>
<td>−144.6</td>
</tr>
<tr>
<td>B case 10</td>
<td>xxx</td>
<td>−233.1</td>
</tr>
<tr>
<td>B case 11</td>
<td>xxx</td>
<td>−138.2</td>
</tr>
<tr>
<td>A case 12</td>
<td>xxx</td>
<td>−7.7</td>
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<tr>
<td>B case 12</td>
<td>xxx</td>
<td>−7.7</td>
</tr>
<tr>
<td>C case 12</td>
<td>xxx</td>
<td>−7.7</td>
</tr>
</tbody>
</table>

Fig. 4. Network for company A with six connections (case 1) (flows are in T/h, numbers of pipes are in brackets, dash lines are connections going to the discharge).
companies A and B and 10 for company C, see Table 5), case 8 with the same relative gain in GEC (compared with case 5) for each company, and also the number of connections less equal to 26.

The results are displayed in Table 5, where the gains in GEC are computed by using case 1, then case 5 as a basis. Case 5 being the basis of comparison, only case 8 provides positive gains for each company (same gain of 13.8%, number of connections equal to 26); it is the best solution for the EIP. The new flowsheet for company A in this solution is depicted in Fig. 7. Compared with case 1, regeneration units (cases 5 and 8) provide very interesting gains (63.9 and 68.8%). The economic interest of regeneration units is evident. It may be interpreted that Table 5 exhibits inconsistent results between waste and regenerated flows for cases B8, (increase (decrease) in waste and increase (decrease) in regeneration). This is yet not the case since included into an EIP a company may reject or regenerate waters coming from other companies.

5.5. EIP with a common regeneration unit (indirect integration, cases 9–13)

The three companies have now an interceptor containing shared regeneration unit(s) and connections between them (see Fig. 5, do not take into account the italic parts). Five cases are evaluated. Case 9 corresponds to an unlimited number of connections and a shared

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**Fig. 5.** Representation of an EIP for the three companies (from Chew et al., 2008) (straight lines: direct integration, dash lines: indirect integration).

**Fig. 6.** Network for company A (case 4) (flows are in T/h, numbers of pipes are in brackets, external connections are in italic).

**Fig. 7.** Network for company A (case 8) (flows are in T/h, numbers of pipes are in brackets, external connections are in italic).
regeneration unit of type I. In case 10, the number of external connections between companies is limited at two pipes and a shared regeneration unit of type I is used. Case 11 concerns an EIP involving an interceptor containing the three types of regeneration units, each company can choose two units among the three possible ones, and unlimited number of connections. Case 12 is deduced from case 11 by restricting the total number of connections to 26 (as in cases 7 and 8) and assuming the same gain for each company (compared with case 5), and finally in case 13, the same gain for each company is also imposed but the total number of connections is arbitrarily increased to 31.

Compared with case 5, only case 13 gives a positive gain for each company (3.6%), but compared with the best solution, case 8, found in the previous example the gain for each company is negative (−11.7%). In conclusion, the EIP involving an interceptor is not economically profitable.

5.6. Discussion

This study shows first that regeneration units yield very significant gains, and second that these gains can be increased again by a direct integration into an EIP. Finally, the a priori most attractive EIP with an indirect integration (interceptor sharing regeneration units) does not succeed in improving the previous solution. The best EIP (case 8) is shown in Fig. 8 (the connections to the waste are not reported), and the flowsheet of company A in this EIP is depicted in Fig. 7.

6. Computational aspects

For all the cases, the problem dimensions are displayed in Table 7. When passing from a DWN problem (case 1) to EIP problems, the dimensions strongly increase. However due to the linear formulation this increase has not much influence either on the problem resolution, or on the CPU time (the computations were carried on an Intel Duo Core 2.53 GHz, RAM 3.45 Go). The MILP problem is solved with the solver CPLEX 11.2.1 of the GAMS package.

<table>
<thead>
<tr>
<th>Problem</th>
<th>Continuous variables</th>
<th>Integer variables</th>
<th>Constraints</th>
<th>CPU time (s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Case 1</td>
<td>173</td>
<td>47</td>
<td>214</td>
<td>0.063</td>
</tr>
<tr>
<td>Case 2–4</td>
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<td>255</td>
<td>900</td>
<td>0.109</td>
</tr>
<tr>
<td>Case 5–8</td>
<td>1164</td>
<td>357</td>
<td>1312</td>
<td>0.140</td>
</tr>
<tr>
<td>Case 9–13</td>
<td>1164</td>
<td>357</td>
<td>1319</td>
<td>0.250</td>
</tr>
</tbody>
</table>

7. Conclusions

In the first part of the paper, a methodology taking into account only the single contaminant case is implemented. A MILP formulation is used to solve the problem. Biobjective optimization of the fresh water flow rate at the network entrance and the water flow rate at regeneration unit inlets, parameterized by the number of connections in the network, is carried out. A strategy based on the global equivalent cost (GEC) and equivalent number of connections (ENC) allows identifying the best practical solution combining moderate GEC, few connections and non null flow rates in the connections, among the theoretical ones displayed on Pareto fronts.

This MILP approach is then implemented to optimize an EIP involving three companies. From several analyzed scenarios, it can be deduced that the best solution is an EIP with direct integration: each company owns its regeneration unit, same gain for each company and restricted number of connections. Compared with the case of companies without EIP and without regeneration unit, the gain in GEC is 68.8%, and compared with the case of companies without EIP, but with their own regeneration unit, the supplementary gain in GEC for each company is 13.8%. This study shows first that regeneration units yield very significant gains, and second that these gains can be increased again by a direct integration into an EIP. Finally, the a priori most attractive EIP with an indirect integration (interceptor sharing regeneration units) does not succeed in improving the previous solution. Using different criteria (GEC, connections number, non null flow rates in the connections), a best practical solution is defined for each case. Moreover, after optimisation, the gain for each case is calculated and each company in the EIP can decide to connect to the EIP or not. Of course, the
calculated gain is different in each case, so it is easier to choose the type of connections. Due to the MILP problem, it is possible to add some technical constraints without any size limitations.

Few studies were realized on the technical constitution of an EIP, and even less in the framework of multiobjective optimization, while the problem is by nature a multiobjective one, combining economical and ecological objectives. Furthermore, in a recent study Sakr et al. (2011) identify seven success and limiting factor for EIPs development. The present study comes within the second one "Added economic value", and fills partially the existing gap in the literature.

References