Abstract—The installation of a condition monitoring system (CMS) aims to reduce the operating costs of the monitored system by applying a predictive maintenance strategy. However, a system-driven configuration of the CMS requires the knowledge of the system kinematics and could induce a lot of false alarms because of predefined thresholds. The purpose of this paper is to propose a complete data-driven method to automatically generate system health indicators without any a priori on the monitored system or the acquired signals. This method is composed of two steps. First, every acquired signal is analyzed: the spectral peaks are detected and then grouped in a more complex structure as harmonic series or modulation sidebands. Then, a time-frequency tracking operation is applied on all available signals: the spectral peaks and the spectral structures are tracked over time and grouped in trajectories, which will be used to generate the system health indicators. The proposed method is tested on real-world signals coming from a wind turbine test rig. The detection of a harmonic series and a modulation sideband reports the birth of a fault on the main bearing inner ring. The evolution of the fault severity is characterized by three automatically generated health indicators and is confirmed by experts.

Index Terms—Condition monitoring, fault diagnosis, harmonics, sidebands, signal processing, tracking, wind turbines.

I. INTRODUCTION

CONDITION monitoring systems (CMSs) are designed to determine the health of a given system and to reduce the operating costs by allowing a predictive maintenance strategy. They are more and more commonly used, especially in wind turbines [1], [2] which have relatively high maintenance costs due to their hard-to-access remote location. The CMS allows us to increase the energy efficiency of the wind turbine, which makes it economically interesting. The hardware of a CMS is composed of sensors that acquire relevant signals. These signals are real-time analyzed owing to a computing unit which provides system health indicators. Two kinds of analysis methods exist: the system-driven and data-driven ones.

The analysis methods which are the more frequently used are system driven: the health indicators are defined depending on the monitored system kinematics. For example, in the case of bearing fault detection, standard indicators are computed by estimating the energy at the characteristic fault frequencies (ball pass frequencies of the inner/outer ring, ball spin, and cage frequencies). These indicators may be used for manual spectrum comparison [3] but also as features in data mining methods [4], [5] or in a probabilistic model [6] for the bearing diagnosis. In [7], a different part of the system is monitored (the rotor bar), but the approach is the same: the energy at the characteristic fault frequencies is estimated and used for the diagnosis. All of these system-driven methods have a main drawback: each CMS has to be configured depending on the kinematics of the system to monitor. Moreover, a reconfiguration step is needed if a part of the system is changed after maintenance (e.g., replacement of a bearing by another one).

The second class of analysis methods is data driven: the health indicators are derived from the data only, without any extra knowledge about the system. In [8], the empirical mode decomposition is used to extract features, and then, a classifier helps to diagnose the system health. However, the diagnosis is made on one measurement only, without considering the time evolution of the fault. In [9], the concept of intrinsic time-scale decomposition allows us to deal with the nonstationarity in the system operations. At the end, the proposed indicators are time-frequency maps, which have to be manually inspected. Similarly in [10], the choice of the parameters for the multiwavelet denoising is data driven. The fault signature is isolated from the rest of the signal, but the time-domain signature has to be manually inspected or further processed to finally diagnose the fault. In [11] and [12], the wind turbine state variables are used to generate a residual which is then automatically thresholded to detect faults. However, the decision is binary and indicates if a fault is present or not, without providing more information. The same idea is used in [13], where more residuals are generated to identify precisely the defect at a cost of a more computationally consuming algorithm. Moreover, the number of sensors to monitor all of the system inputs and outputs is high and costly.

We propose in this paper a complete generic and data-driven method without any a priori on the measured signals.
This method does not need any configuration and is able to automatically provide system health indicators characterizing the time evolution of a fault. In the case of a system part replacement, the indicators linked to the old part will simply stop, and new indicators will automatically start.

The first step of the proposed method is to analyze each successive signal acquired at different timestamps. An automatic spectral analysis [14] detects and characterizes the different spectral structures in the analyzed signals and gives a snapshot of the system health. These spectral structures can either be single spectral peaks or groups of peaks belonging to the same harmonic series or to the same modulation sideband [15]. Each spectral structure is characterized by several parameters, including the number of peaks, the characteristic frequencies, and the energy.

The second step consists of tracking the spectral structures through the different timestamps to create spectral structure trajectories from which health indicators will be derived. The tracking algorithm proposed in this paper is based on McAulay and Quatieri [16] method which has been originally designed for single peak tracking in speech signals. The method is adapted here to deal with more complex spectral structures such as harmonic series and modulation sidebands. Moreover, to make the method more robust against the possible nondetection of some spectral structures at isolated timestamps, a sleep state adapted from [17] is added. Finally, each parameter of the spectral structures grouped in one trajectory is monitored, and its temporal evolution is used as a system health indicator.

This paper is organized as follows. The main problematics are detailed in Section II. In Section III, the identification of spectral peaks and structures is explained. A time-frequency tracking review in Section IV explains the choices which lead us to the proposed method of Section V. Section VI presents the experiments conducted on real-world signals acquired on a wind turbine test rig to validate the proposed method. Conclusion and perspectives are given in Section VII.

II. Problem Position

To monitor a system, vibration or electrical sensors are placed on the system components where possible changes are indicative of a developing fault. Each sensor acquires $N_s$ signals of duration $\tau$ (in seconds) and denoted by $s^n$, where $n$ is the signal index related to its timestamp $t^n$ defined as the beginning of the measurement (in operating hours). The analysis of the sequence \{ $s^1, s^2, \ldots, s^n, \ldots, s^{N_s}$ \} characterizes the system evolution. Note that the time interval between two successive acquisitions at time $t^n$ and time $t^{n+1}$ is not necessarily uniform and may vary from a few minutes to a few days, depending on the user settings and the operating system conditions.

In this paper, we focus on the identification of the signal evolution in the spectral domain. For example, in the case of vibration signals acquired on a mechanical system, each part of the machine (a gear, a bearing, etc.) generates spectral peaks in the vibration spectrum. The frequency and the number of peaks do not depend only on the system kinematics but also on the system wear. The spectral analysis is thus one way to evaluate the condition of a system.

A spectral analysis of a signal $s^n$ allows us to identify all of the peaks $P^n$ present in the spectrum, with $i$ being the peak index in the list of all of the detected peaks sorted by increasing frequency. Part of these peaks is organized in more complex spectral structures as harmonic series $H^n$ or modulation sidebands $M^n$. The identification of these spectral structures is a crucial step of our proposed method as it increases the amount of information about the system condition.

Between times $t^n$ and $t^{n+1}$, the set of spectral peaks and structures will evolve according to the system operation and condition. Let us assume that this evolution is bounded in an interval whose width will be parameterized according to the spectral resolution of the spectral estimator. Thus, we propose to track each detected peak through all of the signals and to record its trajectory $T^n$. In this paper, the principle of trajectories is extended to harmonic series and modulation sidebands, whose trajectories $T^n H$ and $T^n M$ contain a high amount of information about the long-term system evolution, its wear, and its possible failure.

In order to evaluate the condition evolution of a system, two main steps are required: 1) the detection and the estimation of peaks and spectral structures in signals and 2) the tracking of these peaks and structures through all of the available signals. The next section (Section III) presents shortly the proposed detection and estimation methods. Then, Section IV discusses about the time-frequency tracking methods that explain the path that we followed to propose the time-frequency tracking method detailed in Section V.

III. Automatic Identification of Spectral Peaks and Structures

A CMS records signals of different types, like vibration, acoustic, or electrical signals. In order to extract the spectral peaks and the spectral structures of those different signals in the same manner, we propose to use a generic and data-driven method based on an automatic spectrum analyzer software conceived to be the easiest-to-use. In fact, each step of the spectrum analyzer, illustrated in Fig. 1, is fully automatic and does not need any a priori knowledge or settings. The only action a user needs to do is to provide the signal to the spectrum analyzer. Then, information is extracted from the signal to ease the peak detection. Finally, the list of detected peaks is scrolled to identify the spectral structures present in the spectrum. These steps are briefly explained afterward.

A. Data Validation and Peak Identification

The method presented in this section is part of previous works [14], [18], [19] and is briefly explained here to ease the understanding of this paper.

The acquisition of each signal $s^n$ is validated according to a procedure composed of four tests. This data validation checks that there is no signal saturation and that an anti-aliasing has been correctly used during the acquisition. Moreover, the data validation computes a global signal-to-noise ratio [18] and a nonstationarity rate [18], which should be null for a correct peak identification.
In the case of a nonstationary system like wind turbines, the acquisition process has been adapted to still get stationary signals. The acquisition is made continuously in a circular buffer, but the signal is only recorded once the nonstationarity rate computed on the buffer is lower than a predefined threshold (1% in our implementation). In the case where a rotation speed measurement is also acquired, the threshold is relaxed to a higher value (3%), and the nonstationarities are removed owing to an angular resampling [20]–[22].

With this continuous acquisition system, the number of acquired signals is more than sufficient for wind turbine monitoring. Therefore, a second condition is used to trigger the signal recording: the wind speed has to take a value within a given small range. As a consequence, the number of signals is reduced but is still sufficient for condition monitoring purposes. More importantly, the signals are acquired in approximately the same operating conditions to allow the comparison of a signal to another.

Once the signal $s^n$ is acquired, the peak identification is done in the spectral domain. As defining an optimal spectral estimator for every kind of signals is hardly conceivable, a “multicycle” strategy is then proposed. This strategy uses multiple spectral estimators to take advantage of their different strengths [14]. The spectral estimators and their parameters are chosen owing to the information provided by the data validation.

For each spectral estimator, a peak identification is performed directly on the spectral estimate. First, a series of peaks corresponding to the maxima is extracted from the spectral estimate. Second, due to the estimation, it is clear that some of these peaks are only related to the estimation noise, while others are linked to the underlying signal. Thus, a statistical test is applied on each peak frequency (corresponding to the maximum of the peak) in order to decide whether this peak can be considered as an estimation noise peak or as a signal peak. Third, the detected signal peaks are then classified by comparing the spectral estimate with an oversampled theoretical spectral window related to the spectral estimator used. The objective of the comparison is twofold: first to characterize the spectral peaks and classify it in categories like: sinusoidal wave, narrowband signal, or noise; second to increase the peak frequency precision by minimizing the quadratic error between the peak and the oversampled window [14]. Performing these operations for one spectral estimator constitutes what we call one cycle.

Once every cycle is done, a fusion operation merges the results obtained by the different cycles and creates a unique “spectral identity card” for each detected spectral peak $P_i$. The identity card is composed of several parameters characterizing the detected spectral peak. Among them, one can find the estimated amplitude $a_i$, the estimated frequency $f_i$, and its associated uncertainty $\varepsilon_i$ which is used in the spectral structure identification step. The uncertainty $\varepsilon_i$ is linked to the spectral resolution of the estimators and means that the true frequency of the peak is in the interval $[f_i - \varepsilon_i, f_i + \varepsilon_i]$.

The final list of the detected peaks $P_i$ is ordered by increasing frequency, with $i \in [1, N_P]$ being the index of the peak and $N_P$ being the total number of detected peaks.

B. Harmonic Series Identification

A harmonic series is a group of peaks whose frequencies $f_i$ are the multiple of a fundamental frequency $\nu_j$. Methods to identify harmonic series at the output of a spectral analysis exist in the literature; [23] proposed a method based on statistical tests with an a priori hypothesis which states that the power of the series is decisive for the detection. In [24], the diagnosis of a helicopter unit is done after harmonic identification owing to an underlying model. However, these methods have been proposed for specific applications, and the use of an a priori prevents their use for a generic spectrum analyzer. Moreover, the precision of the peak frequency estimation is limited, and the uncertainty $\varepsilon_i$ defined in Section III-A has to be taken into account during the harmonic search.

In this context, we propose to search the harmonics by frequency interval intersection. Each peak is considered as an interval, and the interval has to overlap with the harmonic frequency interval model in order to be considered as a potential harmonic of rank $r$ of the fundamental frequency $\nu_j$

$$\left[\left(f_i - \varepsilon_i, f_i + \varepsilon_i\right) \cap \left[\nu_j - \varepsilon_j, \nu_j + \varepsilon_j\right]\right] \neq \emptyset$$

peak frequency harmonic frequency model

$$\nu_j \neq 0 \text{ and } r \in \mathbb{N}^*.$$ (1)

If several peaks are candidates to be the rank-$r$ harmonic, the peak with the nearest frequency $f_i$ to the model is selected

$$f_i = \arg \min_{f_k \text{ verifying (1)}} |r \nu_j - f_k|.$$ (2)

Each time a peak is added in the harmonic series, the fundamental frequency $\nu_j$ and its uncertainty $\varepsilon_j$ are refined in order to avoid a too large search interval for high ranked harmonics [15], [25]. Nevertheless, the method also allows harmonics to be absent including the fundamental frequency.
The search for harmonic series is made in an exhaustive way. Each detected peak $P_i$ is considered as a potential fundamental frequency. If enough harmonics are found, the harmonic series $H_j$ is then created and characterized. For example, the energy $E_j$ of the series is computed and corresponds to the sum of the peak squared amplitude. As for the spectral peaks, an identity card is defined for every harmonic series

$$
H_j = \{ \{ P_i | P_i \text{ verifies (1) and (2)} \} \}_{i \in [1,N_P]} , \nu_j, \epsilon_j, E_j \}.
$$

(3)

The final list of harmonic series $H_j$ is ordered in fundamental frequency ascending order, with $j \in [1, N_H]$ being the index of the harmonic series and $N_H$ being the total number of detected series.

C. Modulation Sideband Identification

Modulation sidebands are peaks symmetrically and equally spaced around a carrier frequency $\nu_j$. The frequency interval between the peaks is called the modulation frequency $\Delta_j$. Only the peaks which belong to at least one harmonic series are used as potential carrier frequencies. Around these potential carrier frequencies, the search for modulation sidebands is exhaustive [15]. The frequency distances between one potential carrier frequency and each detected peak in a modulation search interval are used as potential modulation frequencies. For each modulation frequency $\Delta_j$, if enough sidebands are found, the modulation $M_j$ is then created.

As for the harmonic series, the identification of the sidebands is made by frequency interval intersection

$$
[f_i - \nu_j - \epsilon_i, f_i - \nu_j + \epsilon_i] \cap [r(\Delta_j - \epsilon_j), r(\Delta_j + \epsilon_j)] \neq \emptyset
$$

peak deviation from carrier frequency modulation sideband model

with $r_j \neq 0$, $\Delta_j \neq 0$ and $r \in \mathbb{Z}^*$

(4)

and in case of multiple candidates, the nearest one to the model is chosen

$$
\begin{align*}
    f_i = \arg \min_{f_k \text{ verifying (4)}} |\nu_j + r \Delta_j - f_k|.
\end{align*}
$$

(5)

A specific identity card for each modulation sideband $M_j$ is also defined, with $j \in [1, N_M]$ being the index of the modulation sideband and $N_M$ being the total number of modulation sidebands

$$
M_j = \{ \{ P_i | P_i \text{ verifies (4) and (5)} \} \}_{i \in [1,N_P]} , \nu_j, \Delta_j, \epsilon_j \}.
$$

(6)

D. Discrete Time-Frequency Map

The identification of spectral peaks and structures is done on every signal $s^n$ acquired by the CMS. In the rest of this paper, the time index $n$ will be added in the exponent position to every notation seen so far. For example, the frequency $f^n_i$ of the peak $P^n_i$ is the frequency of the $i$th peak detected in the spectrum of the signal $s^n$. All of the notations are illustrated in Fig. 2, which represents a time-frequency map where all detected peaks at each timestamp are represented by a marker which is a gray circle for the remaining unassociated peaks, while peaks belonging to the same spectral structure have the same color and shape. This map is discrete in both time and frequency: in time, because the CMS records a signal on an irregular time basis when the system is in operation and, in frequency, because the spectral content is extracted from the spectrum.

IV. TIME-FREQUENCY TRACKING REVIEW

The problematic of time-frequency tracking is already present in the literature, and several tracking methods exist. One of the most widely used is the one developed by McAulay and Quatieri [16], [17], [26], [27]. This method states that a peak at time $t^n$ is associated to a peak at time $t^{n+1}$ if the frequency at time $t^{n+1}$ is inside a search interval centered around the frequency at time $t^n$. This simple but efficient method has been developed for peak tracking only. In [28]–[31], they proposed to predict the future peak frequency at time $t^{n+1}$ based on the peak trajectory in order to place the search interval around the predicted frequency. These methods improve the tracking of fast moving frequencies but need signals regularly acquired. All of these peak tracking methods based on the work of McAulay and Quatieri are not only well suited to analyze audio signals but also for source separation or sound classification.

In [32] and [33], a tracking method based on hidden Markov model is presented. The complexity of the resulting algorithms is high, which make them applicable only over short temporal period or in small spectral band. A maximum a posteriori estimation of one single trajectory has also been proposed in [34]; handling multiple trajectories might be possible if the trajectories are not overlapping. Another method [35] based on parsimony constraints and the Hungarian algorithm [36] tracks spectral lines in spectroscopy at the price of a high complexity.

Meanwhile, other kinds of methods track spectral structures which are groups of peaks representing harmonic series or modulation sidebands (as defined in the previous section). It is particularly the case of pitch tracking methods where the
pitch presents a harmonic structure. In [37], a spectral comb is designed to track the harmonic series of the signal pitch. An extension of the method allows us to track two pitches at the same time but only if their frequencies are not overlapped. In [38], the number of harmonic series tracked can be higher, owing to a constrained classification method. However, the number of series is needed a priori.

In a CMS context, the tracking method should:

1) be able to track both spectral peaks and spectral structures;
2) be as generic as possible, thus necessitating no a priori information;
3) be able to handle a significant amount of signals, with a large number of detected peaks in each signal (about thousands of peaks) and a high number of spectral structures (hundreds of them).

Therefore, the method should have a low complexity in order to avoid long computation time and to be embedded in the CMS. To our knowledge, none of the previously cited methods verifies all of these criteria. In that context, we propose a new tracking method as described in the next section. It is based on the one of McAulay and Quatieri that we have adapted to track both peaks and spectral structures.

The McAulay and Quatieri method has been designed for audio signal analysis divided in short consecutive frames. The length of the frame is short enough (few tens of milliseconds) to consider the audio signal stationary over the frame. Moreover, the frames are temporally contiguous. Thus, the signal content between two consecutive frames is almost the same, which means that the peak frequencies are slightly evolving from one frame to another. This main hypothesis is the key of their tracking algorithm.

The context of condition monitoring is quite different from this one. The signal acquisition is generally not continuous to avoid collecting huge database. Moreover, the acquisition can be done on an irregular temporal basis. This means that the state of the system to monitor could be completely changed between two signal acquisitions. This is troublesome, especially in rotating machines where the characteristic frequencies of the system depend on the rotational speed. Therefore, the main hypothesis to use the tracking algorithm in a condition monitoring context is to acquire the signals in a “constant machine state,” where the operational parameters do not change from one acquisition to the other. For example, the acquisition of signals on a rotating machine should always be done for the same rotational speed, or if not, an angular resampling [20]–[22] should be performed as a preprocess. In this case, the characteristic frequencies of the system will remain the same, and the tracking will be possible.

V. TRACKING OF SPECTRAL PEAKS AND STRUCTURES

The method that we propose tracks the spectral peaks and structures. It is based on the work of McAulay and Quatieri. Their peak tracking method and our proposed modifications will be explained just before describing how we propose to use it to track harmonic series and modulation sidebands. The tracking operations are organized in a specific order to monitor efficiently all of the spectral content. Finally, owing to this tracking, the health indicators are derived based on the estimated trajectories.

A. Tracking of Spectral Peaks

The peak tracking is done pairwise and sequentially; this means that, for each pair of consecutive signals $s^n$ and $s^{n+1}$, the peaks $P^n_i$ detected in the signal $s^n$ (acquired at time instant $t^n$) are associated with the peaks $P^{n+1}_j$ detected in the signal $s^{n+1}$ (acquired at time instant $t^{n+1}$). This process is iterated for each signal index $n \in [1, N_a]$. Moreover, the tracking is done peak by peak, starting from the low frequencies. Suppose that the tracking is done up to time $t^n$ and peak $P^n_{i-1}$. The next peak $P^n_i$ has now to be linked with a peak at time $t^{n+1}$ by a two-step process detailed hereinafter, illustrated in Fig. 3 and resumed by (7).

**Step 1:** A candidate for the association is sought in a research interval $\Delta f$. If there is no candidate like in Fig. 3(a), the trajectory of peak $P^n_i$ dies. If there are multiple candidates, the one with the nearest frequency to $f^n_i$ is elected as the best candidate.

**Step 2:** The best candidate from step 1 has to verify the backward compatibility condition, i.e., the frequency of the candidate peak has to be nearer to $f^n_i$ than to any other detected peaks at time $t^n$. If this backward condition is met, the association is done, and the candidate is added to the trajectory of peak $P^n_i$ [Fig. 3(b)]. Otherwise, there are two cases: either there is no more candidate in the search interval, and the $P^n_i$
The peak frequency comparisons between too consecutive instants \( t^n \) and \( t^{n+1} \) need to run through each list only one time. This means that, if the mean number of peaks per signal is \( N_p \), then approximately \( 2 \times N_p \) comparisons are made for each signal iteration, leading to a complexity in \( O(N_s N_p) \), where \( N_s \) represents the total number of signals.

### B. Tracking of Harmonic Series

There are multiple possibilities in order to track harmonic series through time. In [39], each peak trajectory is independently tracked, and the harmonic series are constructed afterward by grouping the appropriated trajectories. In [28] and [37], constraints of harmonicity are used during the tracking operation; however, only one or two harmonic series can be retrieved.

The method proposed in this paper relies on the fact that the peaks at a given time are already grouped in harmonic series \( \mathcal{H}^n \) of fundamental frequency \( \nu^n_i \) (see Section III-B). To capitalize this previous analysis, the tracking of harmonic series is done globally, which means that, when a harmonic series at time \( t^n \) is associated to another harmonic series at time \( t^{n+1} \), the peaks inside the series are automatically tracked according to their rank in the series. If the rank-\( r \) harmonic is present in the series at time \( t^n \), but is not at time \( t^{n+1} \), the trajectory goes to a sleep state.

In order to track the harmonic series, the peak tracking strategy described in Section V-A is applied to the set of fundamental frequencies of all harmonic series \( \mathcal{H}^n \). This structural approach is illustrated in Fig. 5, which highlights the robustness of the proposed global approach; the tracking is efficient even if the peaks are missing in the harmonic series and even if the fundamental frequency has been detected.

### C. Tracking of Modulation Sidebands

The tracking of modulation sidebands seems a little more complex because each modulation sideband \( \mathcal{M}^n_i \) is characterized by two parameters to track, namely, the carrier frequency \( \nu^n_i \) and the modulation frequency \( \Delta^m_i \). However, the carrier frequency is already tracked during the harmonic series tracking. In fact, as explained in Section III-C, each carrier frequency is necessarily a peak belonging to a harmonic series. Therefore, the peak trajectories \( T^p_i \) constructed during the harmonic series tracking correspond already to the carrier frequency trajectories.

It is then possible to track the modulation sidebands inside each carrier frequency trajectory owing to the method presented in Section V-A. The peaks are replaced by the modulation sidebands around the carrier frequency trajectory and the peak frequency by the modulation frequency \( \Delta^m_i \) of the sidebands.

As for the harmonic series, a modulation sideband is a group of peaks. Once a modulation sideband is tracked between two times \( t^n \) and \( t^{n+1} \), the peaks inside the modulation are automatically tracked according to their modulation frequency.

### D. Feature Extraction

Trajectories of different spectral structures have been identified. From these trajectories and according to the type of trajectory dies [Fig. 3(c)], or there is at least one other candidate in the search interval, and the association is done with it [peak \( P_j^{n+1} \) in Fig. 3(d)].

The backward compatibility condition is satisfied when an association is valid forward and backward in time. The condition to verify is expressed as \( \delta a < \delta b \) with \( \delta a = |f^n_i - f_j^{n+1}| \) and \( \delta b = |f_j^{n+1} - f_j^{n+1+1}| \).

Note that all of the peak parameters are known (estimated in Section III-A) and the only searching parameters to set are the search interval \( \Delta f \). In order to be as generic as possible, \( \Delta f \) is chosen as a multiple of the spectral resolution, which only depends on the signal length and the spectral estimator. Empirically, \( \Delta f \) has been chosen as ten times the spectral resolution, which corresponds to the best compromise between the trajectory stability and a slight frequency evolution.

To sum up, the peak trajectories are constructed sequentially with

\[
P_j^{n+1} \in T^p_i \text{ if } f^n_i - \frac{\Delta f}{2} \leq f_j^{n+1} \leq f^n_i \frac{\Delta f}{2} \\
\text{with } f_j^{n+1} = \arg \min_{k=1, ..., N_p} |f^n_i - f_k^{n+1}|, \text{ and } |f^n_i - f_j^{n+1}| < |f_j^{n+1} - f_j^{n+1+1}|. \tag{7}
\]

In the original method proposed by McAulay and Quatieri, a third step considers the remaining unassociated peaks at time \( t^n \) by starting new trajectories with them. However, this may induce trajectories composed of only one isolated peak, which increases artificially the total number of trajectories. To modify this third step, we propose to create a new trajectory only if at least two successive peaks are included in it. The consequence of this modification is that some detected peaks may remain isolated and belong to none of the trajectories after the time-frequency tracking.

Moreover, the original method is not robust against a mis-estimated peak in frequency at a given time, as the trajectory directly dies. To solve this, we propose to introduce a sleep state as described in [28]. It means that a trajectory can fall asleep and wake up, as long as the sleep duration is not too long. Otherwise, if the sleep duration exceeds a certain duration (two successive processing temporal windows in our context), the trajectory finally dies. This principle is illustrated in Fig. 4.

The tracking algorithm proposed here requires simple operations and can therefore deal with a high dimension of peaks and signals. In fact, as the lists of peaks are already sorted, the
spectral structure, trends are automatically derived by linking the characteristics associated to each spectral structure [see (3) and (6)]. Thus, in the case of harmonic trajectories, the number of harmonics in the series, the energy, and the fundamental frequency are used as system health indicators. The indicators derived from a modulation trajectory will be similar: the number of sidebands in the modulation, the energy, and the modulation frequency. Examples of these indicators are given in the last section of this paper.

**E. Full Tracking Algorithm**

In order to track all of the spectral content without redundancy in the peak tracking, our method is organized as follows: 1) identification of the harmonic series trajectories \( \mathcal{T}_H \) (Section V-B); 2) identification of the modulation sideband trajectories \( \mathcal{T}_M \) (Section V-C); and 3) tracking of the remaining peaks (Section V-A). The so-called remaining peaks are the peaks which, after harmonic series and modulation sideband tracking, are not yet in any trajectories. Then, the final step consists in 4) extracting system health indicators from the identified spectral structure trajectories (Section V-D).

As the tracking algorithm works in a sequential way, it is easy to process the data online. Each time a new signal is acquired, steps 1), 2), and 3) are iterated on this new signal to extend the trajectories. Then, step 4) updates the system health indicators.

**VI. EXPERIMENTS**

The proposed tracking method has been tested on real-world signals recorded over a wind turbine test rig, developed within the frame of the KAStrian project. This section starts with a brief introduction of the wind turbine test rig in Section VI-A and ends up with the obtained results, already presented in [40]. The first main bearing has been dismantled after the first signs of the fault, while the second main bearing has been fully damaged up to totally stopping the normal operation of the rig. These results are presented in Section VI-B and C, respectively.

**A. Experimental Setup: The Wind Turbine Test Rig**

The test rig based on a wind turbine kinematics is designed at a smaller scale (10 kW). Instead of the blades, a geared motor generates the main shaft rotation (around 20 r/min). A multiplier increases the rotational speed with a ratio of 100:1, allowing the generator to operate around 2000 r/min.

To accelerate the wear phenomena, the main shaft bearing can be loaded with axial and radial forces. Moreover, the test rig can run in two modes: the deterioration mode and the measurement mode. The working conditions for the deterioration mode are nonstationary, as the motor speed is programmed to simulate real wind speed profiles in order to apply more realistic constraints on the mechanical elements. On the contrary, during the measurement mode, the working conditions are stationary to immediately meet the constant machine state hypothesis. Measurements in nonstationary conditions are also possible but require preprocessings as described in Section III-A to meet the needed hypothesis for the tracking operations.

The test rig is an experimental platform monitored owing to several sensors, including accelerometers, thermocouples, torquemeters, tachometers, and voltage and current probes. This exhaustive monitoring allows us to test different diagnosis methods (not only the one described in this paper). For example, in [41], the voltages and currents are used for the electrical diagnosis of the test rig, while in [42], they are used for detecting rotor eccentricities. To test the method proposed in this paper, we will focus on three accelerometers taking place on the main bearing: one accelerometer in the axial direction (+x) and the other two in the radial direction (+y and −z). Fig. 6 illustrates the position and directions of the accelerometers.

The vibration signals are acquired while the test rig working conditions are stationary. The conditions remain the same throughout all of the acquisition times. The hypothesis of constant machine state is therefore met. The vibration signals are acquired at different timestamps \( t^n \) of the main bearing life (counted in operating hours), and the signal duration is the same for each acquisition: \( \forall n, \; t^n = 150 \) s. The signals are acquired at a sampling frequency of 39 062.5 Hz, chosen as high as possible in this experimental setup to avoid losing any high-frequency information that might appear. However, a lower sampling frequency would still have been enough to monitor the test rig.

![Fig. 5. Tracking of harmonic series. Spectral peaks are represented by circles, while fundamental frequencies are represented by squares. (a) Peaks belonging to the same harmonic series have the same color. Gray peaks do not belong to any harmonic series. (b) Harmonic series trajectories. Spectral peaks are represented by their fundamental frequencies. (c) Tracking of fundamental frequencies is done; the harmonic series associated take the same color. (d) Peaks in harmonic series are automatically tracked according to their rank in the harmonic series. The line is solid if the rank is present in both harmonic series at times \( t^n \) and \( t^{n+1} \); otherwise, the line is dotted.](image-url)
B. Medium Degradation of the Main Bearing

Each of the 3 accelerometers recorded 12 vibration signals during the main bearing wear test. On average for each signal, 19,400 peaks were detected and grouped in 750 harmonic series and 21,500 sidebands. If these numbers seem large, one has to remember that the identification methods of Section III are applied without any a priori on the signals. In this context, the detection thresholds are voluntarily low in order to avoid missing any peak or structure. However, the number of identified structures could be decreased by providing the system kinematics.

For the radial accelerometer in the (−z) direction, the tracking operations created 1084 harmonic series trajectories, 564 modulation sideband trajectories, and 9327 trajectories among the remaining peaks. From each of these trajectories, trends are automatically generated according to the characteristics of the tracked structure.

One trajectory deserves a particular attention: harmonic series trajectories with a sudden increase in energy around 203 operating hours. The fundamental frequency of this trajectory is 2.72 Hz, and the harmonic series energy, shown in Fig. 7, evolves from 0.011 up to 1.6 $\mu$m$^2$·s$^{-2}$. Such an important increase in energy is a characteristic of a fault.

So far, the proposed method managed to create without any a priori a system health indicator which detects the fault. To complete the diagnosis, information about the system kinematics is necessary in order to identify the mechanical part concerned. In this experiment, such information is available and indicates that the 2.72-Hz frequency corresponds to the ball pass frequency of the outer ring.

The wear test has been stopped after 214 operating hours. The rig was still able to operate, but the main bearing has been dismantled for visual inspection in order to visualize a fault in its early stage. The relevancy of the health indicator generated automatically has been confirmed by the presence of three small flakings on the main bearing outer ring.

This interesting system health indicator is part of a long list of generated indicators. In order to deal with this long list, the following reasonable hypothesis is made: the indicators computed on a healthy system will not vary much, while the indicators computed on a faulty system will evolve drastically. Accordingly, for a full automatic system health diagnosis, further work will focus on identifying automatically the evolving indicators which are the most interesting ones. The use of asymmetry or relative increase coefficients on the indicators shows some potential for classifying the indicators but has to be further developed.

The results of the other radial accelerometer (+y) and the axial one (+x) for this wear test will not be presented here as they show high similarity to that of the radial accelerometer (−z) and they confirm the already presented diagnosis.

C. Full Degradation of the Main Bearing

In this second experiment, a second main bearing, with a different kinematics, has been highly damaged up to totally stopping the normal operation of the rig. At the end of the wear test, the main bearing has been disassembled and visually inspected.

For the accelerometer in the +y direction, 17 vibration signals were recorded while the main bearing wore. For each signal, the number of detected peaks is varying around 19,000. These peaks are organized in approximately 600 harmonic series and 12,000 modulation sidebands, owing to the methods presented in Section III. After the tracking operations, we get 828 harmonic series trajectories and 9373 modulation sideband trajectories. Among the remaining peaks, 12,406 trajectories have been created.

One of the trajectories deserves a special attention. It can be observed at the top of Fig. 8 which represents a discrete time-frequency map where all of the detected peaks are symbolized by small gray circles. The top left corner zoom illustrates the peak density. Among these detected peaks, a particular peak at 3.45 Hz is tracked from 44 to 189 operating hours and is represented by bigger blue circles. Around 129 h, this particular peak evolves to become a harmonic series with more and more peaks (see the increasing number of blue circles over time). The increasing energy of this trajectory is plotted in the middle of Fig. 8. Moreover, the frequency of the trajectory is slightly decreasing (bottom of Fig. 8).

Moreover, shortly after the transformation of the peak at 3.45 Hz in a harmonic series, modulation sidebands started to appear. A 0.333-Hz modulation frequency around the 3.45-Hz carrier frequency is detected. It is shown in Fig. 9 that, since the apparition of sidebands after 134 operating hours, their number increases accordingly to the severity of the fault.
Fig. 8. Evolution of the inner ring fault on the main bearing, seen by a radial accelerometer. At the top, all detected peaks are represented by small gray circles on the time-frequency map. Blue and bigger circles belong to the same harmonic series trajectory linked to the main bearing fault. Below, two trends of the harmonic series are plotted: the energy increases while the fundamental frequency is slightly decreasing.

Fig. 9. Evolution of the number of modulation sidebands around the slowly evolving carrier frequency starting at 3.45 Hz. The modulation frequency is equal to 0.333 Hz.

This 3.45-Hz frequency corresponds to the ball pass frequency of the inner ring. The apparition of harmonics and sidebands at 129 and 134 operating hours, respectively, are first signals of a fault birth. The increase in both the energy and the number of sidebands characterizes the evolution of the fault and its severity. This increase in energy is distributed over the fundamental frequency and all its harmonics [43], hence the increasing number of detected peaks in the series as they start to have a higher level than the noise spectrum. Finally, the slightly decreasing frequency is another characteristic of a bearing fault and is explained by the fact that the inner ring wear generates slipping.

Another harmonic series trajectory deserves also some attention. As illustrated in Fig. 10, the energy of the series starts increasing around 144 operating hours, i.e., 15 h after the first signs of the fault on the inner ring. The fundamental frequency of this series is 2.54 Hz and corresponds to the ball pass frequency of the outer ring. This increase indicates that the severity of the fault is becoming more and more serious as the fault is spreading from the inner to the outer ring.

The combination of these four automatically generated indicators (the energy and the frequency of the harmonic series at 3.45 Hz, the number of sidebands around the carrier frequency of 3.45 Hz, and the energy of the harmonic series at 2.54 Hz) mirrors out the failure and confirms the value of the proposed method that works in a data-driven way.

It is also possible to see in Figs. 8 and 9 that, around 163 h, the harmonic series is not detected. In fact, this signal was highly nonstationary due to a high impulse in the vibrations. As a consequence, the spectral analysis was not able to identify correctly the spectral peaks and structures for this particular signal. However, the tracking of the harmonic series was not stopped, owing to the sleep state. The sleep state on the energy, the frequency, and the number of modulation curves is represented by a dotted line.

VII. CONCLUSION

A data-driven method producing system health indicators has been proposed in this paper. The method is composed of two main steps. First, the spectral content of each signal is identified without any a priori on the monitored system or the acquired signals. The spectral peaks are identified and grouped in structure as harmonic series or modulation sidebands. Second, these spectral peaks and structures are tracked through all of the available signals. The trajectories constructed during the tracking phase are finally used to automatically generate system health indicators from the structure estimated parameters.

The proposed method is tested and validated on real-world signals, acquired on a wind turbine test rig. The degradation of the main bearing confirmed by mechanical experts has been detected in its early stage by the apparition of a harmonic series and a modulation sideband. The evolution of the fault severity is characterized by three automatically generated health indicators.

Future work will focus on sorting and classifying the generated indicators in order to move forward for a full generic and automatic tool to diagnose a system.

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