Multiscale modeling and experimental analysis of chemical vapor deposited aluminum films: Linking reactor operating conditions with roughness evolution

Ioannis G. Aviziotis\textsuperscript{a,b}, Nikolaos Cheimarios\textsuperscript{c}, Thomas Duguet\textsuperscript{b}, Constantin Vahlas\textsuperscript{b}, Andreas G. Boudouvis\textsuperscript{a,}\textsuperscript{*}

\textsuperscript{a} School of Chemical Engineering, National Technical University of Athens, Heroon Polytechniou 9, 15780 Zografou, Greece
\textsuperscript{b} CIRIMAT, CNRS, Université de Toulouse, 4 allée Emile Monso, BP 44362, 31030 Toulouse cedex 4, France
\textsuperscript{c} Scienomics SARL, 16 rue de l’Arcade, 75008 Paris, France

\textbf{I N T R O D U C T I O N}

The rapid advancement of thin films and coatings technologies promoted their usage in a wide range of applications, e.g. microelectronic devices, solar cells, or biomedical products. Aluminum (Al), the third most abundant element on the Earth’s crust, is used for the fabrication of integrated circuits due to its low electrical resistivity (Lee et al., 2012, 2013, 2014). Moreover it is resistant to corrosion (Hamasha et al., 2011) and to electromigration (Tan and Roy, 2007). In addition it can be combined with other elements for the formation of Al-based intermetallics with many degrees of freedom for the exploration of original properties (Kadok et al., 2015). Various methods are developed for the production of Al and...
Al-containing thin films, among which chemical vapor deposition (CVD) combines high growth rates and conformal coverage of complex surfaces (Thomann et al., 2011). However CVD processed Al films suffer from a rough microstructure, despite efforts made to attenuate it (Vahlas et al., 2001). Microstructural characteristics depend on process conditions (surface temperature, pressure, flow rates, etc.). In turn, they impact the targeted properties such as electrical resistivity (Timal-shina et al., 2015), hydrophobicity (Bormashenko et al., 2006; Bravo et al., 2007) and adsorption of proteins (Rechendorff et al., 2006; Zhdanov et al., 2008). Consequently, the technological implementation of such process with regard to targeted specifications requires the establishment of a robust relation between process parameters and films microstructure, e.g. surface roughness. This can be met through the modeling of the CVD process with the roughness as an output.

For most CVD processes, transport phenomena can be described by macroscopic conservation equations for momentum, mass, energy and species. Gas phase and surface chemistry are described in these models by means of kinetic schemes consisting of elementary reactions. However, the continuum description breaks down as the length scale approaches the surface level. Modeling the surface characteristics, e.g. roughness at the same length scale used to model the bulk phase of a reactor, leads to the loss of any structural information of the evolving surface (Barbato et al., 2007). The limitation on the use of the continuum models for the description of surface processes and the evolution of the surface topography during film growth on initially flat surfaces has led to the development of stochastic kinetic Monte Carlo (kMC) modeling (Battaile and Srolovitz, 2002; Cavallotti et al., 2004; Chatterjee and Vlachos, 2007; Collins et al., 2008; Gillespie, 1977, 2001; Katsoulakis and Vlachos, 2003) and multiscale modeling (Cheimarios et al., 2011; Christofides et al., 2008; Crose et al., 2015; Hu et al., 2010; Lam and Vlachos, 2001; Lou and Christofides, 2003; Rodgers and Jensen, 1998; Zhang et al., 2010). The rates of surface processes, such as adsorption, desorption and surface migration, which are necessary for the kMC model, can be provided by experimental data or from molecular dynamics (Rapaport, 2004) and by density functional theory calculations (Zorn et al., 2009).

In multiscale models, the reactor scale is linked to the surface level through the feeding of computational information. The first efforts for linking deterministic macroscopic models with stochastic kMC models have been made for the CVD of diamond (Battaile et al., 1998; Srolovitz et al., 1997), while tries for the coupling of the two different scales are reported for CVD processes taking place in a vertical reactor without using any specific chemical system (Raimondeau and Vlachos, 2000). In the latter, due to the low concentration of the precursor, the continuum equations are solved decoupled. At the macroscopic level, the one-dimensional partial differential equations provided by the similarity transformation of the mass, momentum, energy and species transport equations are used, whereas only one node of the computational domain is chosen to be used for the kMC simulations. The same model is also used by Lou and Christofides (2003) for the estimation of the surface roughness, where the estimated roughness from the multiscale framework is used as an input to a proportional-integral (PI) controller for the successful regulation of the surface roughness at the desired value.

Multiscale simulations of the CVD of Si have been performed (Masi et al., 2000). In this system, only the species transport equations are solved at the macroscopic level and the developed kMC model does not take into account the formation of dimers which is a characteristic of Si surfaces. The linking between the two scales is performed through the deposition rate, by assuming that it remains unchanged regardless the scale. The same assumption has also been used in a different work for the CVD of diamond (Gruijicic and Lai, 2000). These studies confirmed that process conditions, such as deposition temperature and mass fraction of the precursor at the inlet of the reactor, have a significant effect on the deposition rate and on the surface roughness of the films (Lam and Vlachos, 2001).

More recently, the coupling of different length scales has been attempted for the multiscale modeling of the deposition of Si (Barbato et al., 2007; Cavallotti et al., 2004, 2005). There, the macroscopic model is integrated based on the governing conservation equations, while the kMC model takes into account the adsorption of multiple molecules and the formation of dimer structures. Finally, multiscale frameworks are also developed for plasma-enhanced CVD (PE-CVD); for instance, the formation of Si thin films for solar cells (Crose et al., 2015) involves a macroscopic model that consists of the 2-dimensional solution of the continuum equations and a hybrid kMC which accounts for more events on the surface, such as hydrogen abstraction (Tsakikis et al., 2013).

Multiscale frameworks offer a basis for the control of the operating conditions at the reactor scale through regulation of surface micro-(nano)features such as roughness and porosity. In Christofides et al. (2008), the multiscale model considers substrate temperature as the manipulated input parameter for the tailoring of the surface roughness. In Hu et al. (2010), film thickness, roughness and porosity are simultaneously regulated using the concentration of the precursor at the inlet of the reactor as the manipulated parameter. Finally, precursor concentration and modulation of the substrate temperature are used as inputs in Crose et al. (2015) for the control of the physisorption of surface radicals and consequently for the control of film growth rate and roughness.

The multiscale computational framework described in the present contribution is based on the assumption which has already been adopted in the past (Masi et al., 2000) according to which the deposition rate remains unchanged regardless the considered scale. At the macroscopic level, steady-state, 3D simulations are performed for the solution of the governing equations and the computational information which is fed to the nanoscale is the mass fraction of the Al precursor at the surface. The derived kMC algorithm for the description of the microscopic state is developed based on an existing model (Lam and Vlachos, 2001). As a first approach to our experimental measurements and without ignoring the crystallinity and the structure of the developed Al films, we choose to work with a coarse-grained kMC model. The coarse-graining lies in the usage of a simple cubic lattice despite the fcc structure and the (111) orientation of the obtained Al films. The implementation of such an approximation, results in a reduced number of interactions between the surface atoms (five instead of twelve, respectively) and consequently in a reduced computational effort, without sacrificing accuracy. Indicatively, the CPU time required for kMC simulations of the Al surface is approximately 3 h; a similar to the presented kMC model applied in Vlachos (2008), requires 73 min of CPU time, for a 40 x 40 lattice and without incorporating migration events. Acceleration of the computations can be achieved (1.8 min of CPU time, for the latter case) when appropriate methods, such as the r- leap method, are applied (Gillespie, 2001; Vlachos, 2008). In contrast, at the nanoscale level, exact atomistic simulations instead of coarse-grained computations are used for the detailed reproduction of the surface microstructure but highly increase the computational requirements. An example is the homoepitaxial growth of Ag on Ag (111) and the diffusion of Ag monolayer islands on Ag (111) reported by Latz et al. (2012); in this model, the detailed crystallographic structure of Ag along with interactions among second nearest neighbors is used to perform on the fly
simulations for the reproduction of the exact Ag (111) growth. This type of simulations yields an almost hundredfold increase of the computational requirements and self-learning models are applied to reduce the high computational cost (Latz et al., 2012). It will be shown that, within these limitations, the simulated surfaces match well the experimentally determined surface features of the films.

The microscopic algorithm does not explicitly include chemical reactions on purpose; indeed, the chemical information is incorporated in the effective sticking coefficient through a fitting process that correlates this parameter with surface temperature. By fitting the microscopic sticking coefficient to the surface temperature through the macroscopic Al deposition rate (it is recalled that the deposition rate remains unchanged regardless the scale of simulation), we virtually integrate all the steps involved in the chemical reactions (precursor adsorption/desorption, decomposition, products adsorption/desorption, etc.) to end up with an effective sticking coefficient for Al atoms. This particular treatment of the sticking coefficient allows performing fast and accurate computations for the CVD of Al by implementing a procedure which appears as a purely physical one; i.e., involving single Al atomic events only.

Through this framework, we investigate the CVD of Al films from dimethyl-ethylene alane (DMEA) by focusing on growth rate and the surface roughness and we compare our computational results with experimental data obtained in similar conditions. DMEA exhibits relatively high vapor pressure at room temperature facilitating its transport into the reactor, and low process temperature allowing deposition on thermally sensitive substrates. DMEA processed Al films are oxygen/carbon-free (Yun et al., 1998; Yun and Rhee, 1998) and present smoother microstructure than alternative Al precursors such as triisobutyl aluminum (Delmas and Vahlas, 2007). The reaction scheme and kinetics of DMEA has been extensively studied in previous works (Gladefelter, 1993; Jang et al., 1998; Venkateswaran et al., 1996; Xenidou et al., 2010; Yun et al., 1998) and several reaction paths have been proposed (Kim et al., 1998; Nakajima et al., 2003; Simmonds et al., 1994; Xenidou et al., 2007; Yun et al., 1998).

Previous works dealing with the CVD of Al from DMEA focus on the investigation of the kinetic mechanisms and not on the evolution of the microstructure (Aviziotis et al., 2015; Delmas and Vahlas, 2007; Venkateswaran et al., 1996). Thus, it is important in the present case to develop a computational framework which will simulate the surface evolution and reproduce the experimentally determined roughness. As a consequence, the tailoring of final properties of interest is enabled. The evolution of the electrical resistivity (whose low values for a metal are appealing for numerous applications) as a function of process conditions through their impact on the microstructure will be used in this manuscript as a paradigm of this relationship.

The paper is organized as follows: first, we briefly present our experimental work and then, we detail the multiscale framework which enables the simulations at the surface level. Upon the description of the computational framework, we show the results provided by this analysis and we compare them with the corresponding experimental measurements. Finally, we show the dependence of the electrical resistivity of Al thin films on surface roughness and discuss the main findings of this work.

2. Experiments

The CVD of Al thin films is performed in a vertical, cylindrical, stagnant flow, warm wall, stainless steel reactor which has been previously described in detail (Xenidou et al., 2010). 20 × 10 × 1 mm² silicon coupons were cut from 4° Si (100) wafers (Siltronix). They are etched in a (1 ml HF:10 ml H₂O) bath for 1 min, sonicated in an acetone and ethanol bath for 5 min, dried in Ar flow and baked in a furnace at 60 °C for 20 min. In each experiment three substrates are placed horizontally at the center (0 mm), the edge (24 mm) and at an intermediate location (17 mm), on a 58 mm diameter susceptor (substrate holder) heated by a resistance coil gyred just below the surface, where a regulating thermocouple is also attached. Surface temperature T_s is calibrated under primary vacuum by attaching a second thermocouple to the surface of a dummy Si coupon. In the presence of a perforated shower plate which is facing the substrates, a homogeneous gas distribution is ensured, in contrast to a large recirculation zone that sets in when the shower plate is absent. The 60 mm diameter shower plate consists of 1450 holes of 0.76 mm diameter each. DMEA, is supplied by NanoMePS in a specifically designed glass bubbler equipped with a 3-valve stainless steel bypass system. It is maintained at 3 °C permanently; i.e., below the freezing point of the compound, thus strongly limiting its degradation (Jang et al., 1998). It is thermally regulated to 7 °C during experiments. At this temperature, the partial pressure of DMEA is 0.7 Torr (Jang et al., 1998). Pure nitrogen (99,998%, Air Products) is fed through computer-driven mass flow controllers. Experiments are performed in fixed conditions, namely total pressure of the reactor P_rat = 10 Torr, thermal regulation of the lines T_lines = 100 °C and of the walls of the reactor T_walls = 75 °C, while the N₂ dilution gas flow is (Q(N₂) = 294 sccm) and the N₂ carrier gas flow through the precursor (Q(DMEA) = 294 sccm) equal 305 and 25 standard cubic centimeters per minute (scm), respectively. Considering the relation proposed by Hersee and Ballingal (1990), these conditions yield a maximum flow rate Q(DMEA) in the input gas, equal to 2 sccm.

Independent experiments are performed at eight different T_w, in the range 139–241 °C. Deposition time is 1 h and deposition rate is evaluated directly by weight difference of the substrates before and after deposition, using a microbalance (Sartorius) with ± 10 μg accuracy. Three independent weight measurements are carried out before and after the experiment and their average value is considered. The maximum (minimum) deviation from this average value is estimated by the difference between the minimum (maximum) value before the experiment and the maximum (minimum) value after the experiment. Hence, the average value of the weight lies always within the limits of the maximum and minimum deviations.

Surface roughness is determined with an optical interferometer ( Zygo NewView 100) allowing measurements of average roughness down to 0.1 nm and peak-to-valley heights of up to several mm (Seah et al., 2006). Thus, the method is appropriate to quantify the roughness of Al films for which the root mean square (RMS) roughness is less than 1 μm. We report RMS roughness of samples located at the edge of the susceptor averaged on three different points of each sample surface, since we have observed from the experimental work that the deposition rate of samples at this position best match the theoretical trend of an Arrhenius plot (Aviziotis et al., 2015). Finally, the electrical resistivity of Al thin films is measured in a home-made resistivity apparatus based on the four-point probe method (Samolir et al., 2010).

3. Multiscale analysis

The multiscale computational framework is sketched in Fig. 1. It shows the linking of the reactor scale (macroscale) with the surface topology of the film, developed on an initially flat surface. The term “linking” is used instead of coupling, since we apply a one-way communication between the two scales involved; upon convergence of the iterative solution of the discretized governing partial differential equations, the macroscopic model feeds the
microscopic algorithm with the computed mass fractions of the precursor, thus launching the simulation of the surface evolution. The effect of microscopic features on macroscopic phenomena is not a matter of investigation in the present case. In the next subsections, we discuss the computational aspects for the two different scales.

3.1. Macroscopic modeling

A 3D model of the CVD reactor is built, based on the governing equations describing transport phenomena and chemical reactions inside the reactor. Continuity, momentum, energy and species conservation equations augmented with realistic boundary conditions (Chelmarios et al., 2010; Deen, 1998) are discretized in 3D and solved at steady state with the commercial software Ansys/Fluent in order to compute the mass fractions of the precursor at the surface. The set of governing equations is described in details elsewhere (Chelmarios et al., 2010). CVD of Al from DMEAA can be described by two reactions, a volumetric (Eq. (1)) and a surface reaction (Eq. (2)) (Han et al., 1994; Yun et al., 1998), as follows:

\[ \text{DMEAA}_{g}\rightarrow\text{AlH}_{g}+\text{DMEA}_{g}, \quad (1) \]

\[ \text{DMEAA}_{g}\rightarrow\text{Al}_{s}+\text{DMEA}_{g}+\frac{3}{2}\text{H}_{2}g. \quad (2) \]

here DMEA denotes the dimethylethylamine ((CH\(_2\))\(_2\)CH\(_2\)N) ligand, which, in the case of reaction (2), is rapidly desorbed from the surface together with molecular hydrogen (Nakajima et al., 2003). For both reactions, a first order Arrhenius kinetics is implemented and the reaction rate, \( r_{\text{kin}} \), is calculated from Eq. (3).

\[ r_{\text{kin},i}=k_{0,i}\exp\left(-\frac{E_{a,i}}{RT}\right)C_{\text{DMEA},i}, \quad (3) \]

where the index \( i \) represents either the volumetric or the surface reaction, \( k_{0} \) is the pre-exponential factor, \( E_{a} \) is the activation energy, \( R \) is the universal gas constant and \( C_{\text{DMEA}} \) is the concentration of the precursor. In a previous work (Aviziotis et al., 2015), the values of the pre-exponential factors and activation energies were determined as \( k_{0,\text{gas}} = 7.39 \times 10^{5} \text{ s}^{-1} \) and \( k_{0,\text{sur}} = 5.858 \text{ m/s} \); \( E_{a,\text{gas}} = 40.006 \text{ kJ/mol} \) and \( E_{a,\text{sur}} = 19.682 \text{ kJ/mol} \), for the volumetric and the surface reactions, respectively. The boundary conditions imposed at the macroscopic level are described elsewhere (Chelmarios et al., 2010) and the parameters \( \sigma \) and \( \epsilon/k \) of the Lennard-Jones potential needed for the estimation of the properties of the gas phase mixture in the CVD reactor are calculated with group contribution methods (Poling et al., 2001).

3.2. Nanoscale model

The model at the nanoscale is stochastic and is based on a KMC algorithm. For the description of surface events during deposition on an initially flat surface, a pseudo-3D stochastic KMC model on a rectangular lattice is developed and the solid on solid approximation (SOS) is adopted (Gilmer and Bennema, 1972). Microscopic events at the surface are modeled as Markov processes by transition probabilities per unit time (Bernd, 2004). The adsorption rate, i.e., the probability of an impinging atom to stick to the surface upon collision, is given by the kinetic theory for ideal gases (Eq. (4)) (Lam and Vlachos, 2001):

\[ R_{s} = \frac{s_{0}P}{C_{\text{tot}}\sqrt{2\pi m_{\text{m}}k_{B}T_{s}}}. \quad (4) \]

here \( R_{s} \) is the adsorption rate, \( s_{0} \) is the sticking coefficient, \( P \) is the partial pressure, \( C_{\text{tot}} \) is the concentration of free surface sites where adsorption events occur, \( m_{\text{m}} \) is the molecular weight of solid Al, and \( k_{B} \) is the Boltzmann constant. For the calculation of \( s_{0} \), we adopt a fitting procedure; the computed deposition rate is compared with the corresponding experimental one for each \( T_{s} \) and each position of the substrates on the susceptor. This comparison provides a 4th degree polynomial relation between \( s_{0} \) and \( T_{s} \) (Eq. (5)) which is used during microscopic simulations. The fitting is performed within the Matlab software with a polyfit function procedure.

The sticking coefficient is a technical term which is used in the literature to illustrate the efficiency of the process towards film growth; it depends on all process parameters (e.g., temperature, pressure, chemistry) and varies as a function of operating conditions (Vahlas et al., 1998). In the present model, the implementation of such a relation for \( s_{0} \) materialized by Eq. (5), provides a correlation between the sticking coefficient and the deposition temperature while implicitly integrating chemical reactions in the microscopic algorithm. In other words, we simulate the CVD process by performing physical vapor deposition microscopic calculations.

\[ s_{0} = -3.7316 \times 10^{-4} \times T_{s}^{4} + 6.7438 \times 10^{-5} \times T_{s}^{3} - 4.5612 \times 10^{-2} \times T_{s}^{2} + 13.69 \times T_{s} - 1538.6 \quad (5) \]

The given dependence of \( s_{0} \) on \( T_{s} \) is valid only for the temperature range used in this work, as the fitting is based only on experimental results obtained in this range. The graphical illustration of Eq. (5) is presented in Fig. 2. It appears that increase of \( T_{s} \) results in the increase of sticking coefficient.

This correlation has already been observed in the literature (Kim et al., 1991; Matsuda et al., 1990; Raupp and Cale, 1989;

![Fig. 1. Schematic description of the multiscale framework: the reactor scale (macroscale) applies the experimental operating conditions to simulate the transport phenomena and feeds the microscopic model with the computed mass fractions at the surface (nanoscale). The deposition rate remains unchanged regardless the simulated scale.](image-url)
and can be explained by the low pressure (flux-limited regime) (Yanguas-Gil et al., 2009), by the positive apparent activation energy of the process (Raupp and Cale, 1989) and by the absence of a secondary species which would operate as an inhibitor for the reaction (Yanguas-Gil et al., 2009).

Finally, the concentration of the sites on the surface is considered to be $10^{19}$ sites/m$^2$ while partial pressure is calculated based on the mass fraction of the precursor provided by the macroscale. At this point, we assume that the precursor which reaches the surface and is available for the surface reaction, is converted totally to Al atoms, since all the chemical information is incorporated in the sticking coefficient.

The desorption rate depends on the local activation energy. In the computational framework, we consider interactions only among the nearest neighbors, five in the present case, since a simple cubic lattice is adopted. In this first-nearest neighbor interaction (Gilmer and Bennema, 1972), the probability of an adatom reaching the surface to perform a microscopic event depends only on the atom of the bottom layer and the four atoms of the same layer that surround the selected adatom.

The desorption rate is calculated from Eq. (6).

$$R_{d}(n) = \nu_0 \exp\left(-\frac{nE}{k_BT}\right)$$

with $E$ the single bond energy, $\nu_0$ the frequency factor and $n = 1, 2, \ldots, 5$ the number of nearest neighbors. The desorption energy of an adatom from the surface is taken to be 77.19 kJ/mol (Rodgers and Jensen, 1998), while for the frequency factor a typical value of $10^{12}$ s$^{-1}$ is chosen based on literature (Albano et al., 2013).

Surface migration is modeled as desorption followed by re-adsorption and its transition probability is given by:

$$R_{m}(n) = \nu_0 \exp\left(-\frac{nE}{k_BT}\right)$$

where $\nu_1 = \exp\left(\frac{F - E_{m}}{kT}\right)$ is a pre-exponential factor associated with the energy difference that an adatom on a surface has to overcome for hopping from one lattice site to an adjacent one, in the zero adsorbate concentration limit. For simplicity, the migration frequency, $\nu_1$, is taken to be equal to that of desorption (Eq. (6)). $E_{m}$ is the migration energy. Since the initial Si surface is covered quickly by Al adatoms, we only consider the migration energy corresponding to the diffusion of Al on Al which equals 6.465 kJ/mol (Papanicolaou et al., 2001). Within the model, this migration energy accounts for both in-plane (intralayer) and across step edges (interlayer) diffusion. In such a way, we implicitly assume a Schwoebel-Ehrlich (ES) barrier equal to 0. The zero ES value is adopted also in previous works (Huang et al., 1998; Liu et al., 2002), where an atomistic simulator for the 3D growth of Al is applied and a small effect has been observed for crossing Al (111) steps, except for very low temperatures. In the present study, appropriate simulations performed in the investigated temperatures (139–241 °C), indicate that the number of surface migration events is negligible compared to adsorption events, thus validating the ES=0 assumption. However, in agreement with results reported for Al growth (Liu et al., 2002; Stumpf and Scheffler, 1996) and for Ag and Fe growth (Evans et al., 2006), at lower temperatures the rougher growth is attributed to the existence of a small ES barrier. Indeed, the ES energy barrier may not be neglected at sufficiently low process temperature.

The time step of the method is given by:

$$\Delta t = -\frac{\ln(\xi)}{R_{tot}},$$

where $\xi$ is a random number in the (0, 1) interval and $R_{tot}$ is the total transition probability per unit time which is expressed as:

$$R_{tot} = R_dN_f + \nu_0[1 + \nu_1] \sum_{n=1}^{5} N_s \exp\left(-\frac{nE}{k_BT}\right),$$

with $N_f$ the total number of active sites on the surface of the simulated lattice and $N_s$ the amount of atoms with $n$ nearest neighbors.

It should be noted that among the $R$-quantities, only adsorption is fitted to experimental data; migration and desorption are not. Their relative importance on the RMS roughness is discussed below.

The surface is initially flat and it is updated after every adsorption, desorption, or migration event. For simulations, periodic boundary conditions are used, i.e., for every atom which moves out of the boundary of the computational domain, there is an atom which enters the domain from the opposite boundary of the lattice. Since the adsorption probability is site independent, the surface atoms are grouped into classes according to their number of nearest neighbors. The total probability for a given class is given by Eq. (9). The transition probabilities are computed $a priori$ and every kMC trial is successful. After each event, time evolution is performed in a continuous way based on the duration of the event.

The structure of the kMC algorithm is presented in Fig. 3. It starts by selecting a random number. Based on its magnitude, a microscopic event (adsorption, desorption or migration) and a class are selected. Subsequently, a site is randomly selected from the class and the microscopic process is finally executed. After each event, the classes are updated and the transition probabilities

![Fig. 2. The dependence of $s_0$ on $T_e$, within the investigated temperature range.](image)

![Fig. 3. Selection of a microscopic event and a class. A class is consisted of a group of atoms according to the number of their first neighbors in order to reduce the computational cost.](image)
are recomputed. This update is of high computational cost, thus it is chosen to be performed locally, around the nearest neighbors of the atom, avoiding the screening of the whole surface. The local update of the algorithm yields important savings in computational time and it is practically independent of the lattice size (Reese et al., 2001).

For the calculation of deposition rates (DR), we simply compute the difference between adsorption and desorption rates:

\[ DR = R_a - R_d. \]  

(10)

In order to calculate the two rates accurately and to reduce noise effects, we use the event-counting method (Lam and Vlachos, 2001), e.g., for the calculation of the adsorption rate we count the events which led to the adsorption of atoms on the surface and this number is divided by the time period within which adsorption events have been performed. Then, surface roughness is determined using the formula of the RMS roughness, shown in Eq. (11):

\[ \text{RMS} = \sqrt{\frac{1}{N_1} \sum_{i=1}^{N_1} (h_{i+1,j} - h_{i,j})^2 + (h_{i-1,j} - h_{i,j})^2 + (h_{i,j+1} - h_{i,j})^2 + (h_{i,j-1} - h_{i,j})^2} \]

(11)

where \( N_i = N_x N_y \) is the lattice size used in this work \((N_x = 120, N_y = 120)\) and \( h_{i,j} \) is the thickness of the film at each lattice site.

Finally, for the estimation of electrical resistivity, we apply the extended Fuchs-Sondheimer model (FS model) (Timalshina et al., 2015), which is described by Eq. (12):

\[ \rho_0 = \rho_{\text{bulk}} \frac{\lambda}{8d} (1 - p) (1 + \alpha \omega^\beta), \]

(12)

where \( \rho_{\text{bulk}} = 2.7 \mu\Omega\text{cm} \) (Giancoli, 2013) is the resistivity of Al, \( \lambda = 5 \text{nm} \) (Kanter, 1970) is the electron mean free path in Al films, \( d \) is the thickness of the film and \( p \) is the specularity parameter ranging from 0 (completely diffuse) to 1 (specular scattering) (Timalshina et al., 2015). The effect of RMS roughness is denoted by \( \omega \) (\( \omega = \sqrt{\text{RMS}} \)) and \( \alpha, \beta \) are additional empirical parameters that can be adjusted to fit the data (Timalshina et al., 2015).

Despite the high film thickness (ca. >500 nm) of our films which affects the outcome of the FS model (Timalshina et al., 2015), we choose this particular model because it takes into account the RMS roughness explicitly. Besides, the purpose of this work is to demonstrate that an integrated multiscale model enables the prediction of the properties of the final film and the detailed modeling of electrical resistivity exceeds this target.

4. Results and discussion

Fig. 4 presents the dependence of the RMS roughness on the temperature for both experimental measurements and computational predictions. The RMS roughness of Al films deposited at the lower \( T_s \) (139 °C) is high (0.6 \( \mu \)m). RMS decreases with increasing temperature and shows a minimum value of 0.15 \( \mu \)m at ca. 198 °C. Above this temperature RMS seems stable. It has been reported that above 200 °C the RMS slightly increases (Yun et al., 1998) but in our case such slight increase would lie within deviation intervals. Surface roughness is closely related to the change of the microstructure of the film. At a surface temperature below 150 °C, the Al film is not continuous and is composed of grains with a broad size distribution, resulting in high roughness. On the other hand, increasing \( T_s \) from 150 °C up to 227 °C results in smoother surface morphology with coalesced grains and decreasing open porosity with increasing deposition temperature. The computational model accurately reproduces the experimental data, since all the predicted RMS values, except for \( T_s = 198 °C \), lie within the intervals of deviations. We assume that there is no physical reason of such an anomalous variation of the RMS at this particular \( T_s \) and its experimental value is attributed to an offset position.

Fig. 5 shows the number of possible surface events (adsorption, migration, desorption) – directly correlated with R-quantities (Eq. (9)) as a function of \( T_s \). It can be observed that in the investigated temperature range, adsorption dominates the process, since the number of adsorption events is much higher than the corresponding number of migration and desorption events. Migration and desorption are enhanced as temperature increases and on the other hand, adsorption is restrained but the difference between them remains high. Despite the predominance of adsorption, the impact of the migration on the behavior of the RMS roughness is...
significant. In particular, it can be seen that as the number of migration events increases, the surface roughness decreases. This behavior is attributed to the fact that at low temperatures, the process is limited by the surface reaction and adsorption on the surface (Aviziotis et al., 2015) which prevents diffusion from disseminating the atoms on the surface. On the other hand, at higher temperatures, diffusion dominates deposition yielding the more uniform distribution of the atoms on the surface; thus, the RMS roughness is reduced. Desorption may affect the RMS roughness in the sense that atoms that desorbed from the surface can re-adsorb in such lattice sites that roughness decreases. The main impact of desorption is on the deposition rate; at high temperatures, where it is observed that desorption events are increased, the Al deposition rate is reduced (Aviziotis et al., 2015; Xenidou et al., 2010).

Fig. 6 shows the simulated surfaces (6a, 6b) and the corresponding experimentally obtained surfaces (6c, 6d) characterized by interferometry. The surfaces are processed at 151 °C (6a, 6c) and 227 °C (6b, 6d) and the surface heights are shown for each temperature. Although we are performing coarse-grained and not atomistic simulations at the nanoscale level, we observe that there are similarities among the simulated and experimental surfaces. Despite the fact that at low $T_s$ the surface seems more homogeneous, the difference between the minimum and the maximum height is bigger and thus, the RMS is higher. On the other hand, at high $T_s$ the surface seems rougher at a large scale but the small differences among the surface heights yield lower RMS values.

Fig. 7 presents the experimentally measured (red points) and the estimated with the multiscale model (black points) electrical resistivity of Al films as a function of the experimental and the simulated RMS roughness. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)
RMS 0.15 μm to ca. 80 μm at RMS 0.6 μm. These values and the observed evolution of the electrical resistivity are attributed to the increased scattering of the rough surfaces and to their significant contribution to the resistivity (Machlin, 2006). Moreover, grain boundary scattering may contribute a significant excess resistivity in polycrystalline Al films, since the grain boundaries do not scatter the conduction electrons (Francombe, 1988). Finally, O contamination within the film can lead to higher resistivity values. The dependence of the electrical resistivity on the RMS roughness has also been reported for other materials (Jang et al., 2005; Timalsina et al., 2015).

As previously mentioned, the extended FS model (Eq. (12)) is applied to estimate the electrical resistivity of Al films, while the thickness and the RMS roughness are provided by multiscale simulations. Concerning the specularity parameter, we assume a completely diffuse scattering from both the top and bottom surfaces of the Al film, that is p = 0, a statement that holds true for surfaces with high roughness (Kanter, 1970). Finally, by fitting the estimated resistivity to the experimental data, we find a = 30, β = 5.6. The physical meaning of these parameters is not clear (Timalsina et al., 2015) and their fit may not be unique. However, we privilege the accuracy of the computed RMS values in order to have a reliable estimation of the electrical resistivity. The estimation of the electrical resistivity with the extended FS model appears to be fairly good with regard to the corresponding experimental measurements and both datasets present the same trend. As roughness decreases, the discrepancy between experimental data and results provided by the multiscale model increases. This is attributed to the fact that in our estimations we do not incorporate any information for grain boundaries or contamination.

The accurate simulation of the surface microstructure and the control of RMS roughness through the variation of the operating conditions of the reactor, enable the control of the properties of the final film, such as the electrical resistivity. Assuming that surface roughness of crystalline materials often corresponds to the existence of grain boundaries, it may account for the increase in electrical resistivity through grain boundaries scattering of the electrons.

5. Conclusions

We experimentally and computationally investigate the RMS roughness and the electrical resistivity of Al films produced by a CVD process from DMEAA. In particular, for the two parameters we compare the experimentally measured values with those obtained by performing multiscale computations. Multiscale computations allow fetching from the surface of the growing film the information needed to compute the aforementioned properties.

The multiscale framework uses a 3D model of the reactor, based on the conservation equations, which computes the mass fractions of the precursor on the vicinity of the substrate. The outcome is fed to a nanoscale model, based on the kinetic Monte Carlo method, which simulates the evolution of the film and computes its surface roughness and its electrical resistivity. The chemical information for the decomposition of the precursor on the surface are incorporated in the sticking coefficient. For the latter, we implement a deposition temperature dependent function by fitting experimental deposition rates at various temperatures and at various positions on the susceptor.

The obtained results are compared with values of surface roughness of Al films processed in the same conditions. The experimentally determined RMS roughness decreases with increasing the surface temperature, from 0.6 μm at 139 °C to 0.15 μm at 198 °C. The calculated RMS values lie within the deviations of experimental measurements. A very good agreement is obtained between the experimental measurements and those calculated by the multiscale framework.

At low process temperature, adsorption dominates the process, while diffusion and migration events are few. Temperature increase results in the enhancement of migration and desorption which in turn results in the decrease of the surface roughness due to smoother distribution of atoms on the surface. Thus, despite the fact that adsorption is fitted to experiments, while desorption and migration are not, the impact of the two latter on the growth of the surface renders an unconstrained multiscale model.

The electrical resistivity of the films increases with increasing surface roughness from 10 μm at RMS 0.15 μm to ca. 80 μm at RMS 0.6 μm, mainly due to the increased scattering caused by rough surfaces and to higher grain boundaries density which results in the entrapment of electrons. The behavior of the electrical resistivity is quantitatively reproduced when the calculated resistivity is correlated with the simulated RMS of the films.

The presented multiscale computational framework can be implemented to perform similar analysis for other materials or for the simulation of similar surface phenomena taking into consideration the formation of more complex structures, such as dimers or trimers. The incorporation of chemical reactions at the nanoscale and the consideration of the crystallographic structure of the Al films (here fcc) within the nanoscale algorithm are under way. Thus, more species could be accounted for, and the simulation of more complex processes and surface features, such as island formation, grain boundaries and height-height correlation could be enabled. Regarding the calculation of the porosity evolution within the film, the SOS approximation should be replaced by triangular lattice models which, in contrast to the SOS models, can accommodate the formation of vacancies. In that case, alternative multiscale methods such as coarse-graining with low-order macroscopic variables or equation-free methodologies will be implemented, to cope with the associated increased computational effort.

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